



DNS on the Evolution of Vortices in the Upper Boundary Layer in Transition



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Submission: June 24, 2018; **Published:** July 18, 2018

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Abstract

The ring-like vortices (or hairpin vortices) are universal vortical structures in late boundary layer transition. They play a very important role in the boundary layer transition process. In this paper, the development of ring-like vortices and the mechanism of sustainability of these vortices in the upper boundary layer are investigated numerically by direct numerical simulation (DNS). Intense interaction among ring-like vortices and the other vortical structures in different vortical packets which generated at different time are observed. It shows that streamwise counter-rotating cores will generate new ring-like vortices and the ring-like vortices become more stronger and raise to the upper boundary layer after mutual interaction and merging. In the meanwhile, the boundary layer of the late transition becomes thicker.

Keywords: Evolution; Transition; Vortical structures; Interaction; Filaments flow; Parameters; Simulation; Instability; Downstream; Aggregations; Transitional flow

Introduction

Experimental and numerical results show that when the ring-like vortex structures (hairpin or Ω -shaped vortices) are formed [1-5], the late boundary layer transition begins. Almost at each transitional stage of a boundary layer, these structures are usually found in larger vortex packages. It has also been found that they are the dominant mechanism of perturbation in the late stages of boundary-layer transition.

It is, of course, very important to understand the formation and evolution of Λ vortex structures (especially the ring-like vortices) and the evolution of Λ vortex packages which is associated with the onset of the flow transition. In order to gain a better understanding of the transition process at the late stage, we used a high-order DNS to study its mechanisms in a boundary layer [6-11]. In our previous work [8], we studied the origin and formation of vortex and ring-like vortex numerically. It is found that the widely recognized process, the self-deformation Λ of vortex into a ring-like vortex, does not exist. The so-called hairpin vortex is actually the combination of separated Λ vortex and ring-like vortex. The Λ vortex in the upstream is not a general vortex tube. Indeed, it is a pair of open rotation cores [8,9]. The roots of Λ vortex are formed by special gathering of vortex filaments. On the other hand, ring-like vortices are formed separately and independently. The ring-like vortices and the Λ vortex roots are

generated separately by different mechanisms. It is confirmed that the shear layer near the top edge of the boundary is unstable and it will produce such ring-like vortex structures [7].

The purpose of this paper is to further study the mechanism of boundary layer growth during the transition. The evolution of ring-like vortices and vortical packets is studied in detail. In Section II, We briefly introduce the case settings and code validation; in Section III, the vortex structure and its mechanisms from our DNS observation are specified; in Section IV, the evolution process and mechanism of ring-like vortex and vortex package are studied. Finally, we give our conclusions.

Case Setup and Code Validation

Case setup

This paper employs DNS to study the transition process on a flat plate. The grid system we used is $1920 \times 128 \times 241$, representing the number of grids in the direction of the streamwise (x), the spanwise (y) and the wall normal (z). In the normal direction, the grid is stretched. In the streamwise and spanwise directions, the grids are evenly distributed. At the inlet, the length of the first grid interval in the normal direction is 0.43 in wall units ($y^+ = 0.43$). Table 1 lists the flow parameters in our simulation, including Mach number, Reynolds number,

etc. Here, x_m represents the distance between leading edge and inlet, L_x, L_y, L_z are the lengths of the computational domain in x -, y -, z - and z - directions, respectively, and is the wall temperature.

Table 1: Flow parameters.

M_∞	Re	x_{in}	L_x	L_y	L_z	T_w	T_∞
0.5	1000	$300.79 \delta_{in}$	$798.03 \delta_{in}$	$22 \delta_{in}$	$40 \delta_{in}$	273.15K	273.15K

By using the Ω visualization method [12], the vortex structures initiated by the nonlinear evolution of T-S waves during the transition are shown in Figure 1. Reference 8-11 give details of the evolution. The formation of ring-like vortex chains coincides with the experimental results [13] and the numerical results of Rist and his co-authors (Bake et al. [14]).

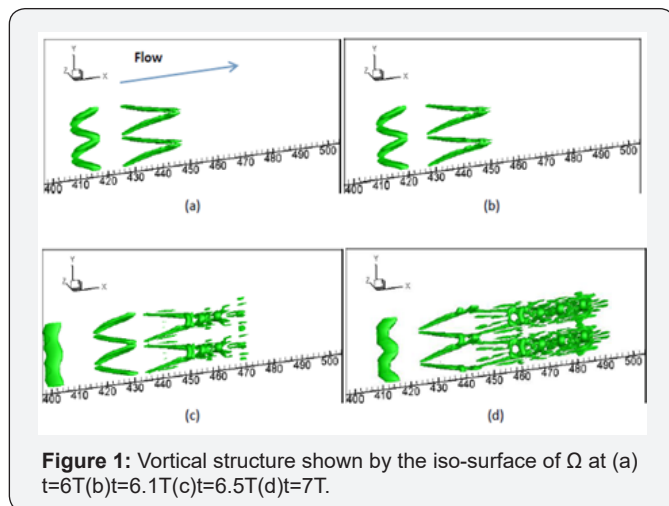


Figure 1: Vortical structure shown by the iso-surface of Ω at (a) $t=6T$ (b) $t=6.1T$ (c) $t=6.5T$ (d) $t=7T$.

DNS Observations on the Vortical Structures in the Boundary Layer

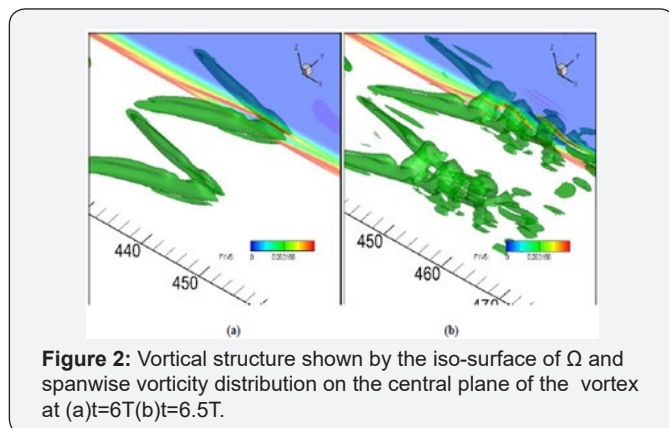


Figure 2: Vortical structure shown by the iso-surface of Ω and spanwise vorticity distribution on the central plane of the vortex at (a) $t=6T$ (b) $t=6.5T$.

Figure 1 shows the vortical structure from our numerical simulation at different time steps are visualized by the iso-surface of Ω ($\Omega=0.5$). At $t=6.0T$, the Λ vortex in Figure 1a is still open at the tip. However, at $t=6.1T$, the first ring-like vortex will soon be generated at the tip of the vortex. After that, more ring-

Code validation

The validations by NASA Langley and UTA researchers of our DNS code can be found in [3-5]. The DNS results are well verified by comparison with theoretical and experimental data and are consistent with other DNS results [6-9].

like vortices are generated above the Λ vortex when it travels to the downstream (see Figure 1c and 1d).

Our previous work [7,8] pointed out that the high shear layer between the roots of Λ vortex (see Figure 2a) is the mechanism by which the ring-like vortices are generated. The high shear is initiated by the input TS waves and formed by rotation effect of the roots of the vortex, especially the ejection which brings the low speed fluid up to approach the high-speed fluids and forms a very strong shear. This very strong shear layer in the middle of Λ -vortex roots is unstable and will break up (see Figure 2b) to several pieces. The ring-like vortices above the Λ -vortex are formed by the breakdown of the shear layer corresponding the Kelvin-Helmholtz instability.

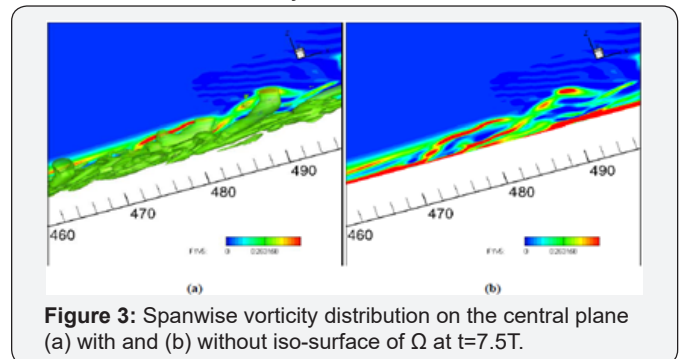


Figure 3: Spanwise vorticity distribution on the central plane (a) with and (b) without iso-surface of Ω at $t=7.5T$.

Once the ring-like vortices are formed, the ejecting and sweeping effect [6,9] becomes more intense as we call the second ejection and second sweep. Along with the streamwise vortical structures (such as Λ vortices), low speed zones will be rolled up successively. On the up-bound of these low speed zones, new strong velocity shear layers will be formed (See Figure 3). Most of these velocity shear layers are unstable, and they will also break down to produce more secondary ring-like vortices. At the same time, the streamwise vortical structures will cause more counter-rotating secondary streamwise vortical structures (see Figure 1d). The energy from the free stream and the spanwise vorticity from the lower boundary layer will contentiously trigger or indirectly produce more vortices under the first generated ring-like vortices [9]. The vortical structure soon becomes very complicated. Each vortex will eventually form a vertical packet in the downstream (see Figure 1d and Figure 4). The vertical packets grow and become wide enough to interact with each other (see Figure 4b). The neighboring vortical packets in the direction of spanwise inevitably converge together.

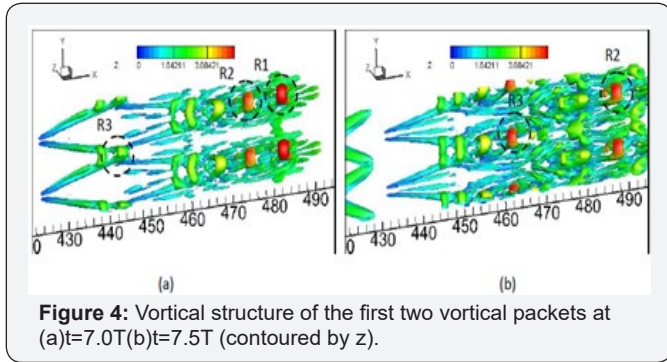


Figure 4: Vortical structure of the first two vortical packets at (a) $t=7.0T$ (b) $t=7.5T$ (contoured by z).

DNS Observations on the Growth of Ring-like Vortices

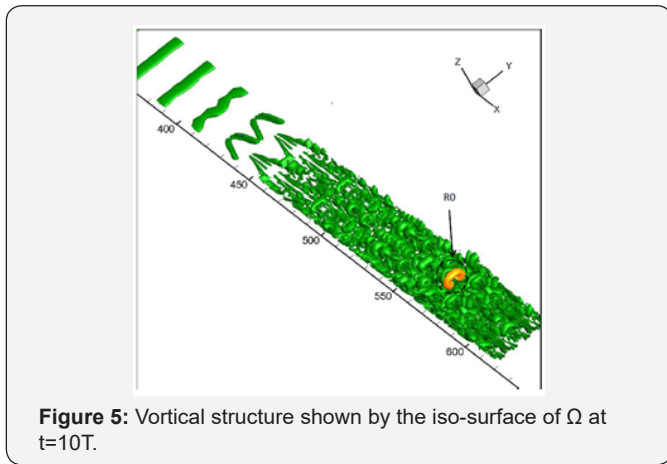


Figure 5: Vortical structure shown by the iso-surface of Ω at $t=10T$.

Figure 5 shows the vortical structure in the boundary layer at $t=10T$. The ring-like vortices at different levels are continually generated. They dominate the development of the boundary layer, especially the upper boundary layer (see Figure 6).

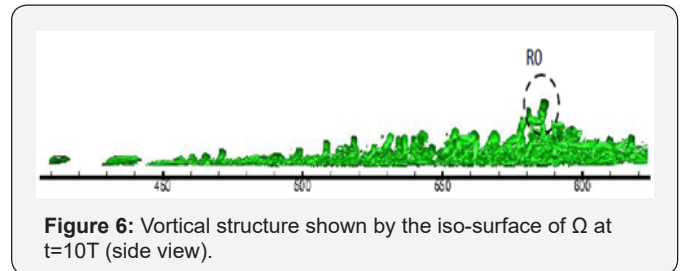


Figure 6: Vortical structure shown by the iso-surface of Ω at $t=10T$ (side view).

As we know, the tilted ring-like vortices will be raised up by self-induction. In such process, however, the ring-like vortices would be weakened due to dissipation in the upper boundary. Figure 7a shows the change of height of the first and second ring-like vortices in Figure 4 (marked as R1 and R2) when they are traveling to the downstream. These two vortices stop raising up in the downstream. Accordingly, the spanwise vorticity at the tops of them keeps decreasing (see Figure 4b). These ring-like vortices will be dissipated eventually. Thus, there must exist other mechanisms for the sustenance and growth of ring-like vortices at the upper boundary layer (see Figure 5). In order to investigate the mechanisms, evolution of the highest ring-like vortex, marked as R0, in Figure 5 and 6 at $t=10T$ is tracked.

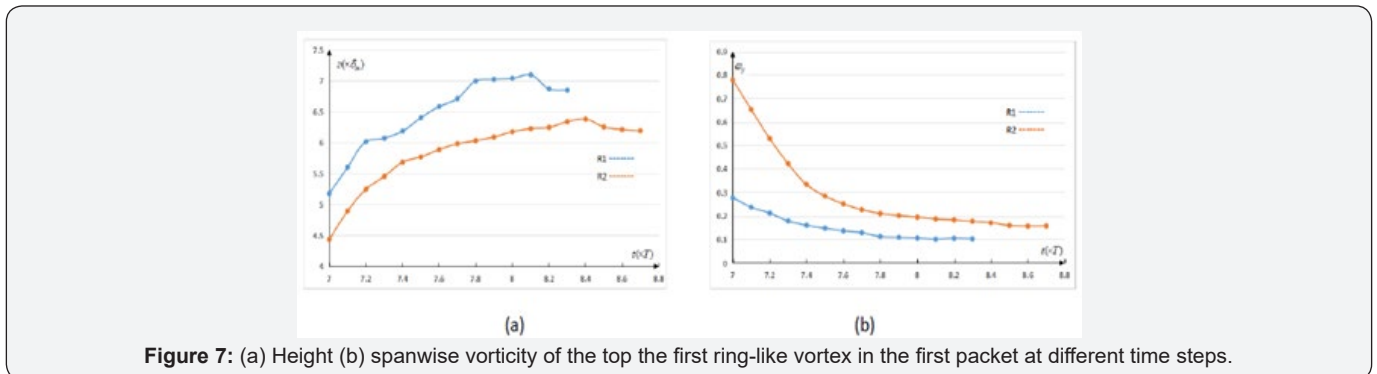


Figure 7: (a) Height (b) spanwise vorticity of the top of the first ring-like vortex in the first packet at different time steps.

Figure 8 shows the evolution of the vortex R0 in Figure 5 at different time steps. Since the ring-like vortices travel faster than the spanwise vortical structures (such as Λ -vortices) in the lower boundary layer, the vortical packet in the upstream will catch up with the ones in the downstream (see Figure 4b). The vortex R3 in the second packet starts to interact with a new generated ring-like vortex (R4 in Figure 8b) in the first packet at $t=8.5T$. Eventually, these two ring-like vortex merges together and become ring-like vortex R0 in Figure 5.

Figure 9 gives the spanwise distribution on the central streamwise plane in the process of forming the large ring-like vortex R0. The tops of the vortex R3 and R4 are circled. It can be seen clearly that the intensity of the ring-like vortex R3 is reduced a lot before it catches the first vortical packet. However, it will be strengthened after entering into the first vortical

packet, especially when the interaction happens with R4 - a new generated ring-like vortex in the downstream. The merge of these ring-like vortices creates a larger and much stronger ring-like vortex-R0 (Figure 9c).

Figure 10 shows the vortical structure in the downstream of the vortex R3 and the distribution of spanwise vorticity on the central plane. It shows that the newly generated ring-like vortex R4 at $t=8.55T$ is generated at the upper bound of a shear layer by the instability of this shear-layer (K-H instability). The shear layer is created by the up-wash effect of the counter-rotating cores (see Figure 10 and 11). This kind of counter-rotating cores are a common vortical structure in the transitional flow (see Figure 4b, 8d and 10a). They are not vortex tubes but still the aggregations of vortical filaments which are similar to Λ -vortices [8]. Strong shear layers are continually formed between these

counter-rotating cores and new generations of ring-like vortices will happen at the upper bounds due to K-H instability (see Figure 10). The existence of streamwise counter-rotating cores and the shear layers is one of the mechanisms for generating and sustaining ring-like vortices in the upper boundary layer in the transitional flow.

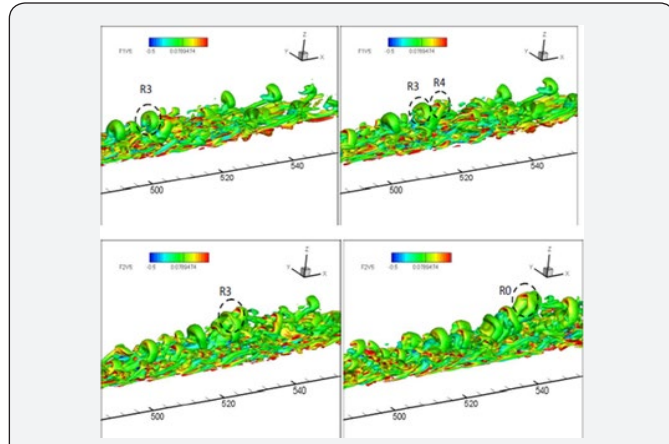


Figure 8: Vortical structure contoured by spanwise vorticity at (a) $t=8.4T$ (b) $t=8.6T$ (c) $t=8.85T$ (d) $t=9.15T$.

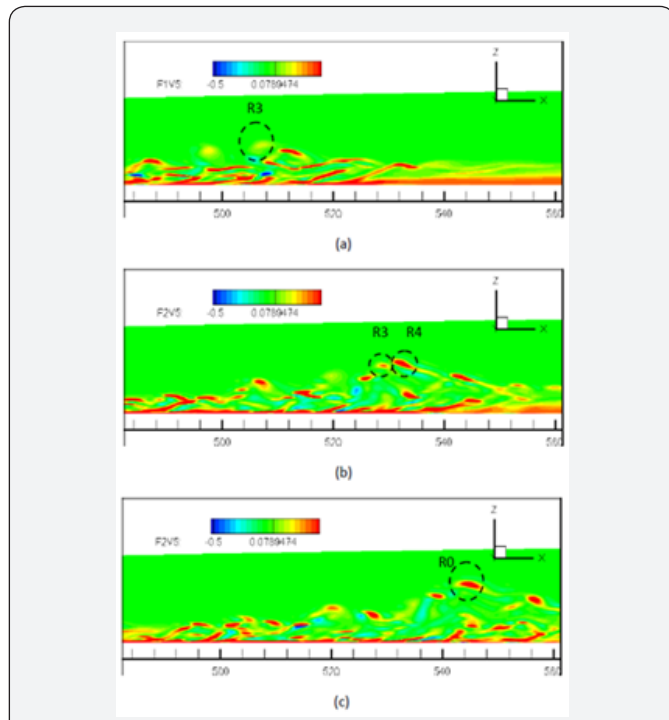


Figure 9: Distribution of span wise vorticity at central stream-wise plane at (a) $t=8.4T$ (b) $t=8.85T$ (c) $t=9.15T$.

Figure 12a gives the heights of the vortex R3 from 7.5T to 9.7T. It shows that this ring-like vortex keeps rising. The height of this ring-like vortex is lower than the vortices R1 and R2 in the first vortical packet at $t=7.5T$ (also see Figure 4). However, it reaches the height of $13.3\delta_{in}$ which is twice as the maximum height of R1 has ever reached. It must be pointed out that, the increase of the height of R3 seems linearly, even after it caught the first vortical packet. There's no jump on the height after the second vortical packet mixed with the first packet. When two vortical packets meet together, the second vortical packet is not

simply pushed up. Complicated interaction among vortices and other vortical structures will happen.

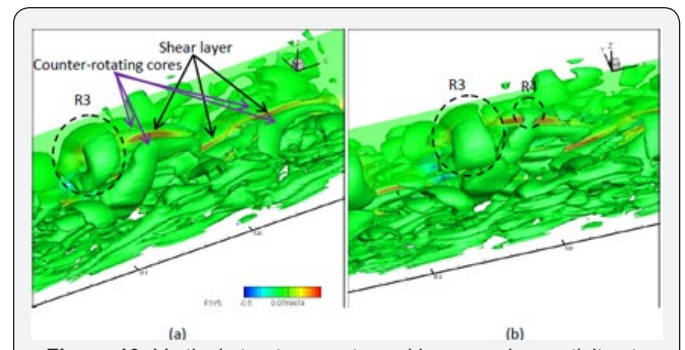


Figure 10: Vortical structure contoured by spanwise vorticity at (a) $t=8.4T$ (b) $t=8.6T$ (c) $t=8.85T$ (d) $t=9.15T$.

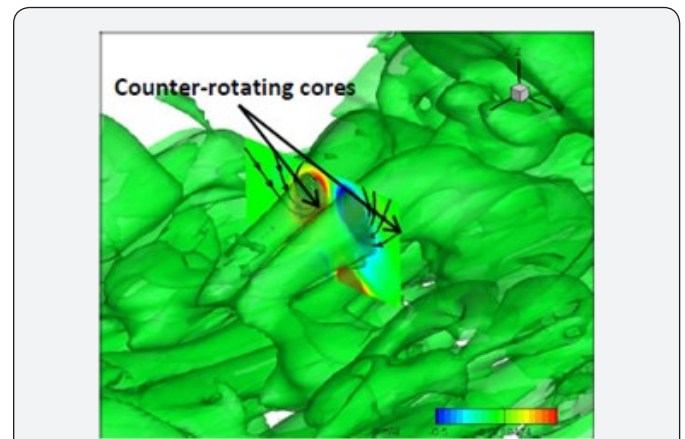


Figure 11: Vortical structure shown by the iso-surface of Ω and distribution of streamwise vorticity at a spanwise plane of at $t=8.45T$.

In Figure 12b, the spanwise vorticity at the top of the ring-like vortex R3 and R4 is provided. It shows that the ring-like vortex R3 is first reduced before it catches the first vortical packet. Then, the intensity of its top become increasing and oscillating. The vorticity increases and reaches a peak when R3 merges with R4 (become R0) at about $t=9.1T$. Of course, when the new generated ring-like vortex R0 keeps arising, it will be reduced again (see Figure 12b).

During the evolution of vortical structures in the downstream, more and more different vortical packets are mixed, some of the ring-like vortices will continually be strengthened by mutually interaction and merging. In the meanwhile, more secondary ring-like vortices and other vortical structures will be created. The boundary layer is thickened gradually during this process. At last, the typical forest of vortical structure will be formed in the boundary layer (see Figure 5). The interaction between vortical packets are very complicated and require further studied in detail.

Conclusion

In this paper, the study on the development of ring-like vortices in the transitional flow by DNS (direct numerical simulation) is given. This includes the mechanisms of the formation of large ring-like vortices in the upper boundary

layer, the mutual interaction among ring-like vortical structures and the increase of boundary layer thickness. It is found that the streamwise counter-rotating cores played a very important role on generating new ring-like vortices in the upper boundary layer. The ring-like vortical structures generated in different time and different packets also interacts intensely. Once the

vortical packets meet together, the ring-like vortices will interact and merge with each other. The strengthened ring-like vortical structures will move towards a higher position and become stronger. The boundary layer thus becomes thicker gradually during the process.

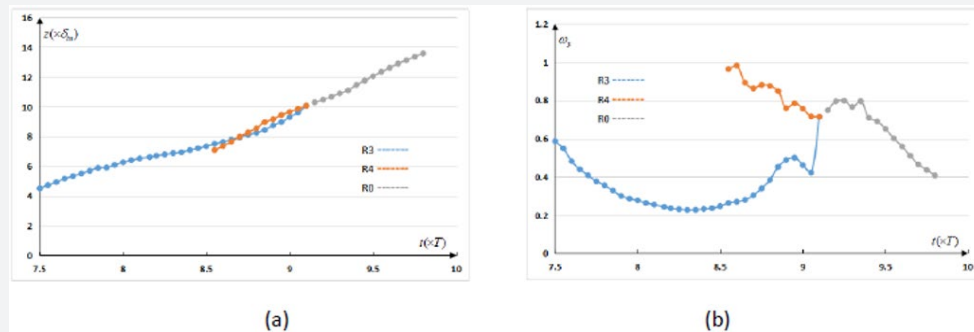


Figure 12: (a) Height (b) spanwise vorticity of the top of the first ring-like vortex in the second vortical packet at different time steps.

Acknowledgment

The authors are grateful to Texas Advanced Computing Center (TACC) for providing computation hours. This work was partially supported by Science and Technology Commission of Shanghai Municipality (Grant No. 13DZ2260900). This work is accomplished by using Code DNSUTA which was released by Dr. Chaoqun Liu at University of Texas at Arlington in 2009.

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 DOI: 10.19080/ETOAJ.2018.02.555582

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