On Generating Electro-Positive Drinking Water

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Abstract
The electrochemical transformation of a drinking water into the positively charged one by means of the galvanic cell with the quasi-equilibrium anode and with the strongly polarized cathode is considered. These electrodes intensively produce hydroxyl radicals in the stream of pure water by the electric current in the cell. The mole fraction \([\text{OH}]\) of the active and short-living radicals is nearly equal to the mole fraction \([\text{H}_2\text{O}^+]\) of hydroxonium ions. These species form the positively charged pair as a hydrated cluster \([\text{H}_3\text{O}^+\text{OH}^-]^{-10^7}\) in liquid water. It is shown that such water is characterized by high concentration of the charged particles \([\text{H}_2\text{O}^+\text{OH}^-]\) and by the shift of oxidation-reduction potential (ORP) into the positive region ORP > 1.0 V.

Introduction
Simple water is described as a dielectric with the wide band gap, \(\varepsilon_{\text{gap}}\), equal to 6.9 eV [1]. It is the energy difference between the highest molecular orbital occupied by electrons and the lowest unoccupied molecular orbital. At the same time, there are two allowed local energy levels in the band gap of liquid water as occupied-by-electrons, \(\varepsilon_{\text{OH}^-}\), hydroxide ion, OH\(^-\), and the vacant one, \(\varepsilon_{\text{H}_2\text{O}^+}\), of the hydroxonium ion, H\(_2\)O\(^+\). These levels are located symmetrically nearby the band-gap middle with the energy difference between them of 1.75 eV [2]. Such the model allows eliminating the inconsistencies of electrochemical properties of these well known charged particles [3] by means of the band theory of water [2].

So, one can use Fermi level, \(\varepsilon_F\), as an oxidation-reduction potential (ORP) [4,5] which indicates the tendency of liquid water to donate or accept the proton. When Fermi level is high, liquid water will donate protons, i.e. that is an antioxidant. Opposite, water will accept protons and will become the oxidant when Fermi level is low [6]. Since electrons cannot occupy the same quantum states, they have to occupy the ones that can accept them. If it is not happening, all the local quantum states (as oxidants) are inactive due to high Fermi level in the band gap of liquid water. For activating oxidizing agents, Fermi level is to shift down at least to the electron level of these species and this is possible only when water becomes hyper-stoichiometric, \(H_2O_{1-z}\) (\(z < 0\)).

From this rule, one can easily get the difference between pH and ORP of liquid water. The first can be changed in stoichiometric water, \(H_2O\) by adding equivalent amount of anions and cations into liquid water. The second can be modified without changing \(\text{pH}\) by electro-oxidizing of pure liquid water in as much as just a little non-stoichiometry of \(H_2O_{1-z}\) is required (\(|z| < 10^{-10}\)) for this and ORP will be sensitive to external conditions and may be changed without visible varying a composition of aqueous solution [6].

At the same time, such water can get the positive electrical charge that gives several unique properties of drinking water responsible for the health benefits: antibacterial and clearing action becomes curative. It is important to correctly estimate a scale of this tendency for generating electro-positive drinking water in practice. This estimate is the subject of the given work.

Non-Stoichiometry of Liquid Water
Allowed local electronic levels in the band gap of liquid water, \(\varepsilon_{\text{H}_2\text{O}^+}\) and \(\varepsilon_{\text{OH}^-}\), can be vacant and occupied by electrons like impurity levels in the band gap of solid dielectric. The molecular carriers of these levels are the attributive species of water as the occupied-by-electrons hydroxide ion, \(\text{OH}^-\), and the vacant one of hydroxonium ion, \(\text{H}_2\text{O}^+\). They are obtained by the chemical reaction of dissociation [7]:

\[
2\text{H}_2\text{O} \leftrightarrow \text{H}_3\text{O}^+ + \text{OH}^- \tag{1}
\]

and their mole fractions \([\text{H}_2\text{O}^+]\), \([\text{OH}^-]\) as the inherent water species satisfy the ratio [8]

\[
[\text{H}_2\text{O}^+] = K_w \tag{2}
\]

with the dissociation constant \(K_w = 10^{-14}\) M\(^2\) at \(T = 298\) K. Their electronic levels, \(\varepsilon_{\text{H}_2\text{O}^+}\) and \(\varepsilon_{\text{OH}^-}\), are symmetrically to the band-gap middle which is Fermi level, \(\varepsilon_F\), of stoichiometric water, \(H_2O\), (Figure 1a) [2]. In non-stoichiometric water, \(H_2O_{1-z}\),
Fermi level, $\varepsilon_F$, is the single-valued characteristic of ORP [5]:

$$\text{ORP} = -\left(\varepsilon_F - \varepsilon_{\text{SHE}}\right)/e$$  \hspace{1cm} (3)

$e$ is the charge of electron and $\varepsilon_{\text{SHE}}$ is the Fermi level of the Standard Hydrogen Electrode (SHE) [7]:

$$2\text{H}_2\text{O} + 2e^- \leftrightarrow \text{H}_2 + 2\text{H}_2\text{O} \text{ (ORP=0V)}$$  \hspace{1cm} (4)

One can see that ORP becomes negative when Fermi level is shifted to the donor level, $\varepsilon_{\text{H}_2\text{O}}$. Thus, this level will be occupied by electrons forming the hydroxonium radicals, $\text{H}_3\text{O}^+$, as strongest oxidants. This transforms water into hyper-stoichiometric state, $\text{H}_3\text{O}^+\text{a}^+\text{c}$ ($z>0$). Opposite in the hyper-stoichiometric water ($z<0$), Fermi level is shifted to the acceptor level, $\varepsilon_{\text{OH}}$, making the positive ORP and forming hydroxyl radicals, $\text{OH}$, as strongest oxidants.

So, Fermi level, $\varepsilon_{\text{F(a)}}$, in hypo-stoichiometric water $\text{H}_2\text{O}_{1-z}$ is defined by the electron population of the donor level, $\varepsilon_{\text{H}_2\text{O}}$, as a molar fraction $[\text{H}_2\text{O}] = \sqrt{\frac{K_{\text{H}_2\text{O}}}{[\text{H}_3\text{O}^+]}}$ where $K_{\text{H}_2\text{O}}$ is the constant of $\text{H}_2$ dissociation in water for forming hydroxonium radicals, $\text{H}_3\text{O}^+$, as hydrated hydrogen atoms, $\text{H}^+\text{H}_2\text{O}$, by reaction:

$$\text{H}_2 + 2\text{H}_2\text{O} \leftrightarrow 2\text{H}_3\text{O}$$  \hspace{1cm} (5)

Fermi level, $\varepsilon_{\text{F(b)}}$, in hyper-stoichiometric water $\text{H}_2\text{O}_{z>0}$ is defined by hole population of the acceptor level, $\varepsilon_{\text{OH}}$, as hydroxyl fraction, $[\text{OH}] = \sqrt{\frac{K_{\text{H}_2\text{O}}}{[\text{H}_2\text{O}]}}$, where $K_{\text{H}_2\text{O}}$ and $K_{\text{H}_2\text{O}}$ are the constants of $\text{O}_2$ dissociation in water with forming hydrogen peroxide, $\text{H}_2\text{O}_2$, as hydrated oxygen atom, $\text{H}_2\text{O}$ and its dissociation:

$$\text{O}_2 + 2\text{H}_2\text{O} \leftrightarrow 2\text{H}_2\text{O}_2$$  \hspace{1cm} (6)

$$\text{H}_2\text{O}_2 \leftrightarrow 2\text{OH}.$$  \hspace{1cm} (7)

The states of liquid water in Figure 1b with Fermi levels: $\varepsilon_{\text{F(a)}}$ and $\varepsilon_{\text{F(b)}}$ are obtained by the standard reactions [7]:

$$2\text{H}_2\text{O} + 2e^- \leftrightarrow 2\text{H}_2\text{O} + \text{H}_2\text{O}_2 \text{ (pH = 7)}$$  \hspace{1cm} (8)

$$\text{O}_2 + 2\text{H}_2\text{O} + 4e^- \leftrightarrow 4\text{OH}^- \text{ (pH = 7)}$$  \hspace{1cm} (9)

at $[\text{H}_3\text{O}^+] = [\text{OH}^-] = 10^{-7} \text{ M}$, $[\text{H}_2\text{O}] = 1.6\times10^{-3} \text{ M}$, $[\text{O}_2] = 2.7\times10^{-4} \text{ M}$, $P_{\text{H}_2} = P_{\text{O}_2} = 1 \text{ atm}$, $T = 298 \text{ K}$ and $K_{\text{H}_3\text{O}^+} \sim 2\times10^{-33} \text{ M}$, $K_{\text{H}_2\text{O}_2} \sim 6\times10^{-33} \text{ M}$ giving $[\text{H}_3\text{O}^+] \sim 2\times10^{-3} \text{ M}$ for the reaction (8) and $[\text{OH}^-] \sim 8\times10^{-33} \text{ M}$ for (9) [2].

It means that the electron level, $\varepsilon_{\text{H}_2\text{O}}$, is mostly vacant as hydroxonium ions, $\text{H}_3\text{O}^+$, due to $\varepsilon_{\text{F(a)}}$ is below $\varepsilon_{\text{H}_2\text{O}}$ (see Figure 1b, left) and the energy level, $\varepsilon_{\text{OH}}$, is fully occupied by electrons as hydroxide ions since this Fermi level is essentially above $\varepsilon_{\text{OH}}$. Fermi level, $\varepsilon_{\text{F(b)}}$, is slightly above the electron level, $\varepsilon_{\text{OH}}$. Therefore it contains holes (the thin dotted blue line in Figure 1b, right) as hydroxyls (OH) but the energy level, $\varepsilon_{\text{H}_2\text{O}}$, is essentially below $\varepsilon_{\text{H}_2\text{O}}$.

Forcedly shifted Fermi level, $\varepsilon_F$, in the band gap of liquid water is determined rigorously by the ratios of mole fractions: $[\text{H}_3\text{O}^+]/[\text{H}_2\text{O}]$ and $[\text{OH}^-]/[\text{OH}^-]$, of the vacant species ($\text{H}_3\text{O}^+$, $\text{OH}^-$) and the occupied-by-electrons ones ($\text{H}_2\text{O}_2$, $\text{OH}^-$) for the energy levels, $\varepsilon_{\text{H}_2\text{O}}$ and $\varepsilon_{\text{OH}}$, in the band gap of liquid water. These ratios are given by Fermi–Dirac statistics which can be simplified to Maxwell–Boltzmann distribution of electrons and holes in the corresponding energy levels [10]:

$$\left[\frac{\text{H}_3\text{O}^+}{\text{H}_2\text{O}}\right] = \exp\left(\frac{-\varepsilon_{\text{H}_2\text{O}} - \varepsilon_{\text{OH}}}{kT}\right)$$  \hspace{1cm} (10)

$$[\text{OH}^-]/[\text{OH}^-] = \exp\left(\frac{-\varepsilon_{\text{OH}} - \varepsilon_F}{kT}\right).$$  \hspace{1cm} (11)

Then, submitting $[\text{H}_3\text{O}^+]/[\text{H}_2\text{O}]$ of the electrode (8) into (10) and $[\text{OH}^-]/[\text{OH}^-]$ of the electrode (9) into (11), we have obtained in [2]: $\varepsilon_{\text{H}_2\text{O}} - \varepsilon_{\text{OH}} = 1.75\text{eV}$ out of the well-known requirement of the chemical stability of liquid water: $\varepsilon_{\text{F(a)}} - \varepsilon_{\text{F(b)}} = 1.23\text{eV}$ [7]. So, $\varepsilon_{\text{H}_2\text{O}} = -5.58\text{eV}$ and $\varepsilon_{\text{OH}} = -7.32\text{eV}$.

Thus, consideration of liquid water in the frame of band theory shows that varying its ORP is the immediate result of Fermi level shift in the band gap. Water becomes an antioxidant, i.e. hypo-stoichiometric, $\text{H}_2\text{O}_{1-z}$, when Fermi level is shifted to the level $\varepsilon_{\text{H}_2\text{O}}$ which is occupied by electrons and hydroxonium radicals (H$_3$O$^+$) are formed. Opposite, in hyper-stoichiometric water ($z>0$), Fermi level is shifted to the level $\varepsilon_{\text{OH}}$ which is occupied by holes and forms hydroxyls. Therefore water becomes oxidant.

Now, we can obtain the dependence of Fermi level on the index, $z$.
of non-stoichiometric water, H$_2$O$_{1-z}$, as the graph represented in Figure 2 [6].

One can see that the region of chemical water stability ($-13 \times 10^{-4} \leq z \leq 10^{-3}$) is shifted to the hypo-stoichiometric state, H$_2$O$_{1-z}$ ($z>0$), which is achieved easier by least shifting of Fermi level from the band-gap middle to the donor level, $\varepsilon_{3HO}$, as well as the hyper-stoichiometric one, H$_2$O$_{1-z}$ ($z<0$), is achieved by a little variation of $z$ to the acceptor level, $\varepsilon_{OH}$. At the same time, Fermi level is shifted in the band gap about 1 eV.

**Electro-Oxidizing of Liquid Water**

Forced oxidizing of liquid water (shifting $\varepsilon_{F}$ down) can be carried out by the electrochemical cell with the voltage of ~2 V between the strongly polarized cathode and the anode at quasi-equilibrium with water [6] under obvious condition [11]:

\[
\frac{[\text{OH}^-]_{c} f_c \frac{d\varepsilon_{\text{on}}}{dz}}{f_a} = [\text{OH}^-]_{a} f_a \frac{d\varepsilon_{\text{on}}}{dz} \tag{13}
\]

at $f_c \gg f_a$. Here index “c” denotes cathode and “a” - anode, $f_i$ is the specific surface of distributed i-electrode, and $\frac{d\varepsilon_{\text{on}}}{dz}$ is the divergence of electric field in this electrode. At these conditions, the external potential applied to the cathode intensively generates hydroxide ions, OH$^-$, in the narrow cathode layer (Figure 3) of chemically unstable water by reactions:

\[
2\text{H}_2\text{O} + e^- \rightarrow \text{H}_3\text{O}^+ + \text{OH}^- \tag{14}
\]

\[
\text{H}_3\text{O}^+ + e^- \rightarrow \text{H}_2\text{O}^+ + \text{OH}^- \tag{15}
\]

Hydroxide ions are discharged to hydroxyls by quasi-equilibrium anodic reaction [12]

\[
\text{OH}^- - e^- \rightarrow \text{OH} \tag{16}
\]

in the bulk anode region (Figure 3). Here, the hydroxonium radicals, H$_3$O, diffused out of the cathode layer donate electrons to hydroxyl radicals by reaction

\[
\text{H}_3\text{O}^+ + \text{OH}^- \rightarrow \text{H}_3\text{O} + \text{OH}^- \tag{17}
\]

All this forms the positive charge in liquid water near the cathode (Figure 3) with the ratio

\[
[H_3O^+] > [\text{OH}] > [\text{OH}] > [H_2O^+] \tag{18}
\]

In contrast to (12) here, the index z of non-stoichiometric water, H$_2$O$_{1-z}$, is defined by formula [11]

\[
z = 0.018\{[\text{H}_3\text{O}^+] + [\text{H}_3\text{O}] - [\text{OH}^-] - [\text{OH}]\} \tag{19}
\]

We have obtained in [11] the z-depended graphs of these species as shown in Figure 4. One can see the equal mole fractions of hydroxonium ions and hydroxyls.
Thus, the ratio (18) indicates the strong acidic reaction of the chemically stable hypo-stoichiometric water containing the large mole fraction of hydroxyls ([OH] ~ 10^{-7} M) as strongest oxidants (see Table 1).

Oxidation potential of chemical oxidants [13].

In this case, the hydroxyl radicals quickly form the solvated acceptors for electrons by reaction

\[ \text{H}_2\text{O}^+ + \text{OH} \rightarrow \text{HO}_2^- \]  

(20)

in the bulk of electrochemical cell due to their very short lifetime (only few nanoseconds) [8].

Figure 4: The mole fractions of the species: H_3O^+, H_2O, OH, and OH^- as the functions of z in the electrochemical cell (see Figure 3).

Table 1: Oxidation potential of chemical oxidants.

<table>
<thead>
<tr>
<th>Oxidant</th>
<th>ORP, V</th>
</tr>
</thead>
<tbody>
<tr>
<td>Hydroxyl radical</td>
<td>2.8</td>
</tr>
<tr>
<td>Oxygen (atomic)</td>
<td>2.42</td>
</tr>
<tr>
<td>Oxygen (molecular)</td>
<td>1.23</td>
</tr>
</tbody>
</table>

Conclusion

The quick response of Fermi level to changing of the water non-stoichiometry, z, takes place in the stoichiometric state (z=0). Just therefore, a little additive of oxidant in pure water changes oxidation-reduction potential (Fermi level) appreciably.

Such the effect may be gotten also by electric oxidizing of pure water in the electrochemical cell with strongly polarized cathode and the anode in equilibrium with the aqueous medium under the condition (13).

The advantages of this approach are the high efficiency of oxidation reaction, the simplicity of the procedure, low cost, and there is no need for special sorbents because pure water itself becomes the agent for oxidizing pollutants. Such water can contain the large concentration of the charged particles ([H_2O_2^+] ~ 10^{-7} M and the oxidation-reduction potential can be in the positive region ORP > 1.0 V.

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References
