

Elastic Buckling Loads of I-Section Steel Columns with a Variety of Web Hole Shapes



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Abstract

The paper presents the behaviour and the elastic buckling loads of I-section steel columns with various web hole shapes. The behaviour of such steel columns is analysed according to two direction axes including the actual axis ($y-y$) and the virtual axis ($x-x$). Based on the behaviour of the I-section steel columns in two axes, the elastic buckling loads are formulated. It is found that the elastic buckling loads of the I-section columns with perforations in the virtual axis are determined with the consideration of shear action effects. Also, the elastic buckling loads of such columns depend on the shapes and dimensions of the web holes as well as the distances between these holes.

Keywords: Elastic buckling loads; I-section steel columns; Web hope shapes

Introduction

Steel members with perforations have been widely used in structural buildings to adapt the technical system requirements, material savings and aesthetic aspects. This steel member type can be seen in many buildings such as Home Place Club or Liverpool Porche illustrated in Figure 1. The appearance of these web holes is convenient to arrange the technical systems such as electricity, water or fire pipes. In terms of economic aspects, this solution allows for reducing the material cost due to the decline of structures' self-weight. Also, the height of section members is found to significantly increase, this helps to rapidly increase member rigidity compared to this of the solid member with the same material expenditure. For architectural requirements, this solution allows structural members to become aesthetic with their own architectural style.

In terms of manufacturing, these perforated steel members can be made by dividing I-sections into two pieces as shown in Figure 2. These two pieces, subsequently, are combined together using welding; this allows the sectional heights of the new members to increase from 1.4 to 1.5 times in comparison with those of original section members. There are also a variety of web hole shapes that can be made to satisfy the usage requirements as shown in Figure 3.

There were a large number of research studies on steel structural members with holes. The effects of various hole shapes on the strengths of stub columns as presented in publications [1-4]. The hole locations and hole lengths were also considered in many previous studies [5-8]. These studies focused on experimental and numerical investigations to investigate the strengths and behaviours of steel members with perforations. The determination of elastic buckling loads of steel members with holes was determined by various methods such as experimental or numerical analyses. In terms of theoretical methods, studies on elastic buckling loads of steel members with perforations remain scarce. The paper, therefore, is aimed to propose a set of formulae to calculate the elastic buckling loads of I-section steel columns with a variety of web hole shapes.

The strength and behaviour of I-section steel columns with perforations

It was found that shear deformations have negligible impacts on the capacities of solid columns, but this has noticeable impacts on the strengths and behaviours of steel columns with perforations [9]. The shear deformations, therefore, are considered in this study to investigate the elastic buckling loads of this type of steel column. The I-section steel columns with perforations can be

assumed as open-web steel columns including two tee branches as shown in Figure 4. Hence, the buckling behaviour of I-section steel columns are analysed in two directions including the actual

axis ($y-y$) and virtual axis ($x-x$). Two types of web holes are considered in this paper consisting of circular and hexagon hole shapes (see Figure 4).



a) Liverpool Porche Building



b) Holmes Place Fitness Club

Figure 1: Several structural buildings using steel members with perforations.

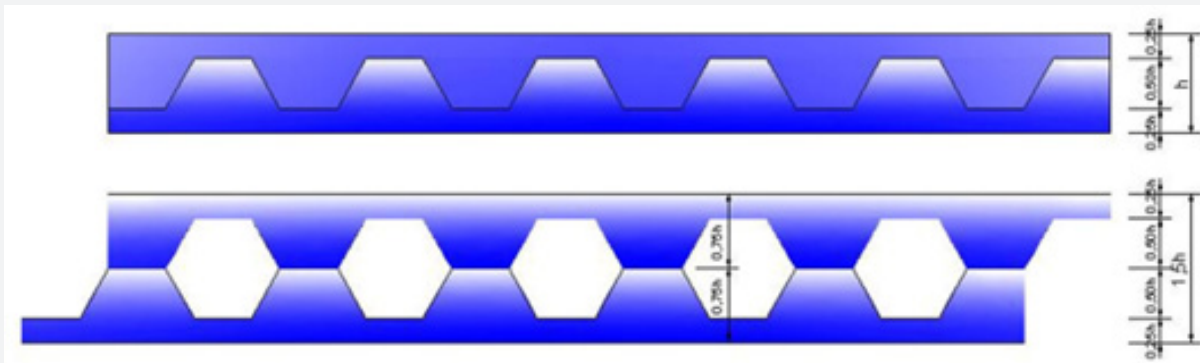
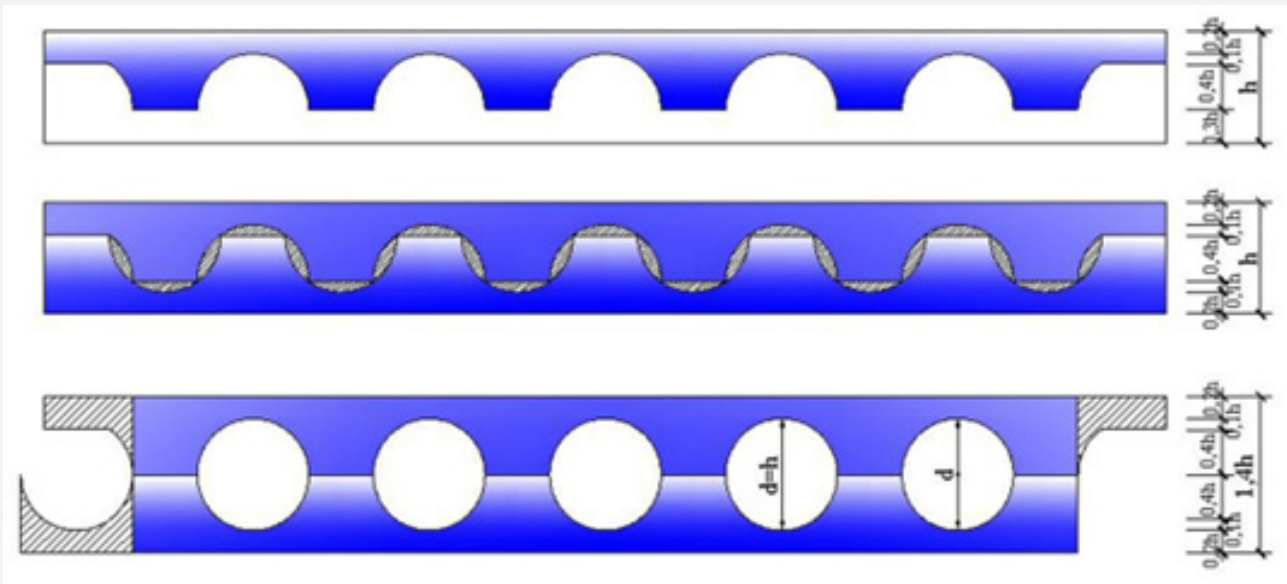
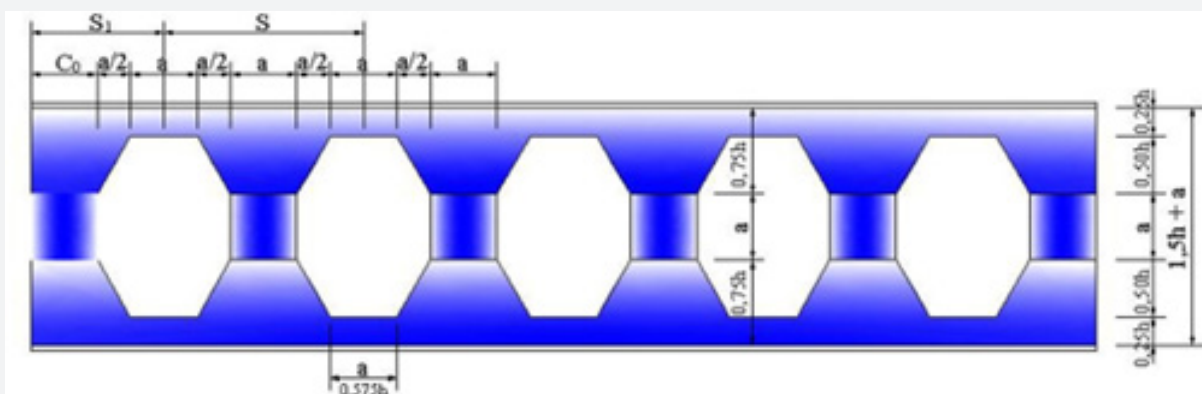


Figure 2: I-section steel members with hexagonal web holes.



a) I section member with circle web holes



b) I section member with octagonal web holes

Figure 2: I-section steel members with hexagonal web holes.

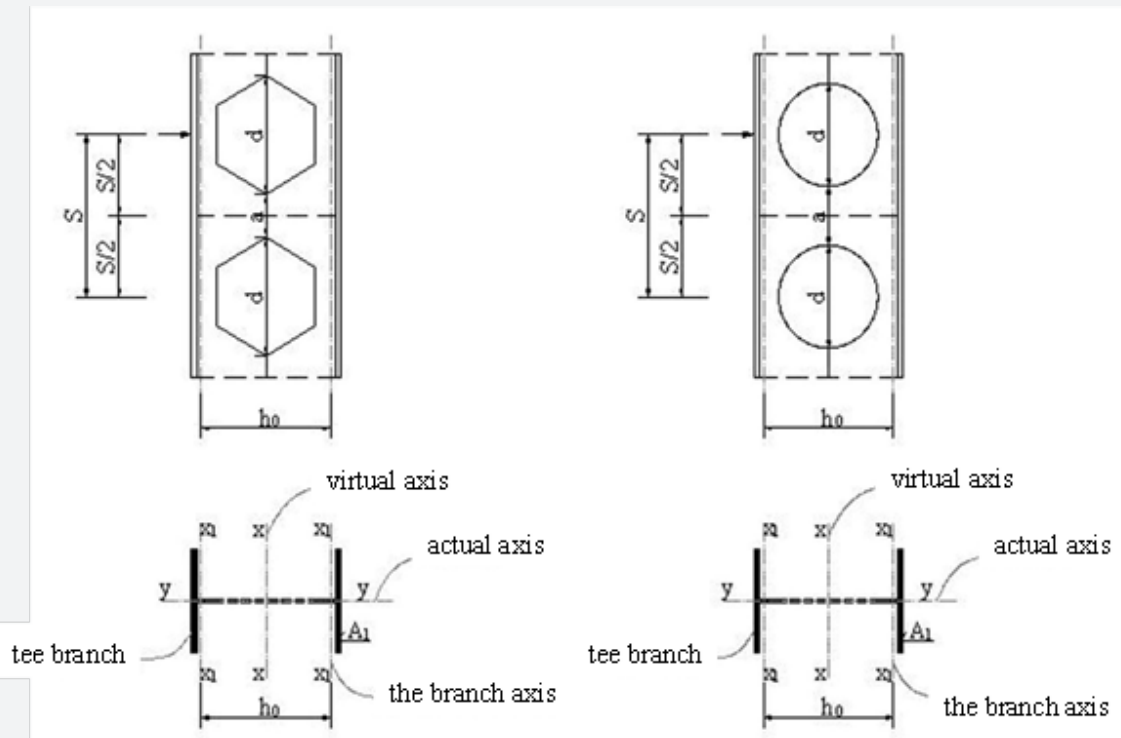


Figure 4: Cellular columns with hexagon and circle holes.

The behaviour of I-section steel columns with perforations about the actual axis (y-y)

If buckling occurred, two tee section branches were bent around the actual axis (y-y). It was found that the connected webs between two branches were not resisted any moments or deformations. These connected webs, therefore, were ignored in the working of this type of column in the actual axis; and, the behaviour of I-section steel columns with perforations can be considered to work as the behavior of two tee solid columns about the actual axes (y-y).

The total area of two tee branches: $A_{ny} = 2.A_1$.

The moment of inertia of two branches about the actual axis (y-y):

$$I_{ny} = 2.I_{y1}$$

The radius of inertia of two branches about the actual axis (y-y):

$$i_y = \sqrt{\frac{I_{ny}}{A_{ny}}} = \sqrt{\frac{2.I_{y1}}{2.A_1}} = \sqrt{\frac{I_{y1}}{A_1}} = i_{y1} \tag{1}$$

The slenderness of I-section steel columns about the actual axis (y-y):

$$\ddot{e}_y = \frac{l_y}{i_y} = \frac{l_y}{i_{y1}} \tag{2}$$

where:

A_1, A_{ny} - section areas of one tee branch and two branches of the perforated columns, respectively;

i_{y1} - the radius of inertia about the $y_1 - y_1$ axis;

I_{y1} - the moment of inertia of one tee branch about the actual axis (y-y).

The behaviour of I-section steel columns with perforations about the virtual axis (x-x)

In the virtual axis (x-x), the I-section steel columns not only resisted stresses due to moments but also shear actions. These shear actions led to the distortions of two tee branches as illustrated in Figure 5. The deformations due to the effects of shear actions had significant impacts on the stability of I-section steel columns with web holes, leading to the reductions of the elastic

buckling loads of this type of column (N_{cr}). The elastic buckling loads about the virtual axis (x-x), therefore, were determined with the consideration of shear action impacts as following Eq. (3) as presented in [9]:

$$N_{cr} = N_E \frac{1}{1 + \gamma_1 N_E} = \frac{\pi^2 EI_{mx}}{l_x^2} \frac{1}{1 + \gamma_1 \frac{\pi^2 EI_{mx}}{l_x^2}} \quad (3)$$

Taking $I_{mx} = i_x^2 A_{mx}$, $l_x = \lambda_x i_x$, Eq. (3) is converted into Eq. (4) as follows:

$$N_{cr} = \frac{\pi^2 EA_{mx}}{\lambda_x^2} \frac{1}{1 + \gamma_1 \frac{\pi^2 EA_{mx}}{\lambda_x^2}} = \frac{\pi^2 EA_{mx}}{\mu_t^2 \lambda_x^2} \quad (4)$$

where:

N_E – the Euler critical strength;

γ_1 – the slippery angle due to the impact of the unit shear

action;

λ_x – the initial slenderness of the I-section column with perforations about the virtual axis (x-x);

$\mu_t = \sqrt{1 + \frac{\gamma_1 \pi^2 EA_{mx}}{\lambda_x^2}}$ – the factor that considers the effects of the connected web deformations due to shear actions.

$\lambda_{td} = \mu_t \lambda_x$ is the equivalent slenderness of the I-section steel columns about the virtual axis (x-x).

The elastic buckling loads and buckling stresses of I-section steel columns with perforations can be determined according to the Euler equation, as follows:

$$N_{cr} = \frac{\pi^2 EA_{mx}}{\lambda_{td}^2}; \sigma_{cr} = \frac{\pi^2 E}{\lambda_{td}^2}; \quad (5)$$

Hence, it is necessary to determine the equivalent slenderness of the I-section steel columns about the virtual axis (x-x) in order to calculate the elastic buckling loads of this type of column.

Determination of the equivalent slenderness λ_{td} of cellular columns with virtual axis x-x

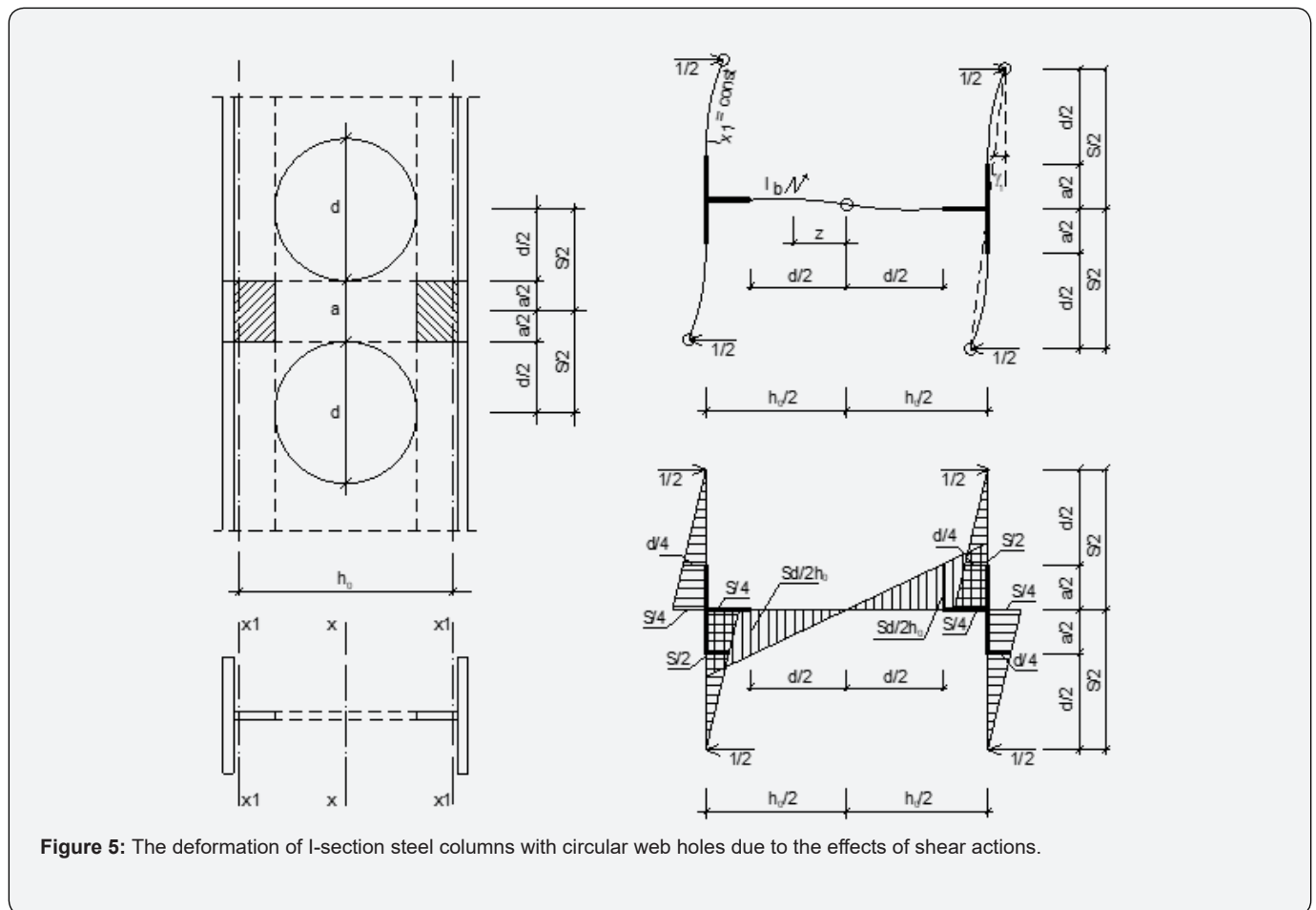


Figure 5: The deformation of I-section steel columns with circular web holes due to the effects of shear actions.

To simplify the procedure in the determination of internal forces and local deformations of I-section steel columns due to the effects of shear actions, the mid-points at the two tee branches between two holes and the mid-points at connected webs having zero moment force were considered as hinges [9]. Intersections between the two tee flanges and the connected webs were considered as highly rigid areas in the analysis (see Figure 5) [10]. The equivalent slendernesses can be determined for two web hole shapes including circular and hexagon web holes.

In terms of I-section steel columns with circular web holes, the highly rigid area was considered as shown in Figure 5. The slippery angle γ_1 is made due to the unit shear force ($V=1$) determined according to the following calculations.

The lateral deformation was determined according to the Veresaghin principles [11] as follows:

$$\ddot{A} = \frac{4}{EI_{x1}} \left(\frac{1}{2} \cdot \frac{d}{4} \cdot \frac{d}{2} \right) \cdot \frac{2}{3} \cdot \frac{d}{4} + \frac{3S^2}{Et_w h_0^2} \int_0^R \frac{z^2 dz}{(a+2R-2\sqrt{R^2-z^2})^3} = \frac{d^3}{24EI_{x1}} + \frac{S^2}{Et_w h_0^2} X = \frac{d^3}{24EI_{x1}} \left(1 + \frac{I_{x1} S^2}{d^3 t_w h_0^2} X \right)$$

where X can be determined as follows:

$$X = \frac{1}{\sqrt{a(a+2d)}} \arctg \left(\sqrt{\frac{a+2d}{a}} \right) \left(\frac{3d^3}{8a(a+2d)} - \frac{3(a+d)}{4} \right) + \left(\frac{3d}{8(a+2d)} + \frac{3d^3}{16a(a+d)(a+2d)} + \frac{3\pi}{16} \right) \text{ Put } n = \frac{I_{x1} S^2}{d^3 t_w h_0^2} X \text{ is the ratio depending on the rigidity of each tee column branch and the dimension of the web holes.}$$

For I-section steel columns with hexagon web holes, the highly rigid areas were illustrated in Figure 6. The slippery angle γ_1 is made due to the unit shear force ($V=1$) determined according to the following calculations.

The lateral deformation was determined according to the Veresaghin principles [11] as follows:

$$\ddot{A} = \frac{4}{EI_{x1}} \left(\frac{1}{2} \cdot \frac{d}{4} \cdot \frac{d}{2} \right) \cdot \frac{2}{3} \cdot \frac{d}{4} + \frac{12S^2}{Et_w h_0^2} \int_0^{b \cos \alpha} \frac{z^2 dz}{(a+2z \tan \alpha)^3} = \frac{d^3}{24EI_{x1}} + \frac{S^2}{Et_w h_0^2} X = \frac{d^3}{24EI_{x1}} \left(1 + \frac{I_{x1} S^2}{d^3 t_w h_0^2} X \right)$$

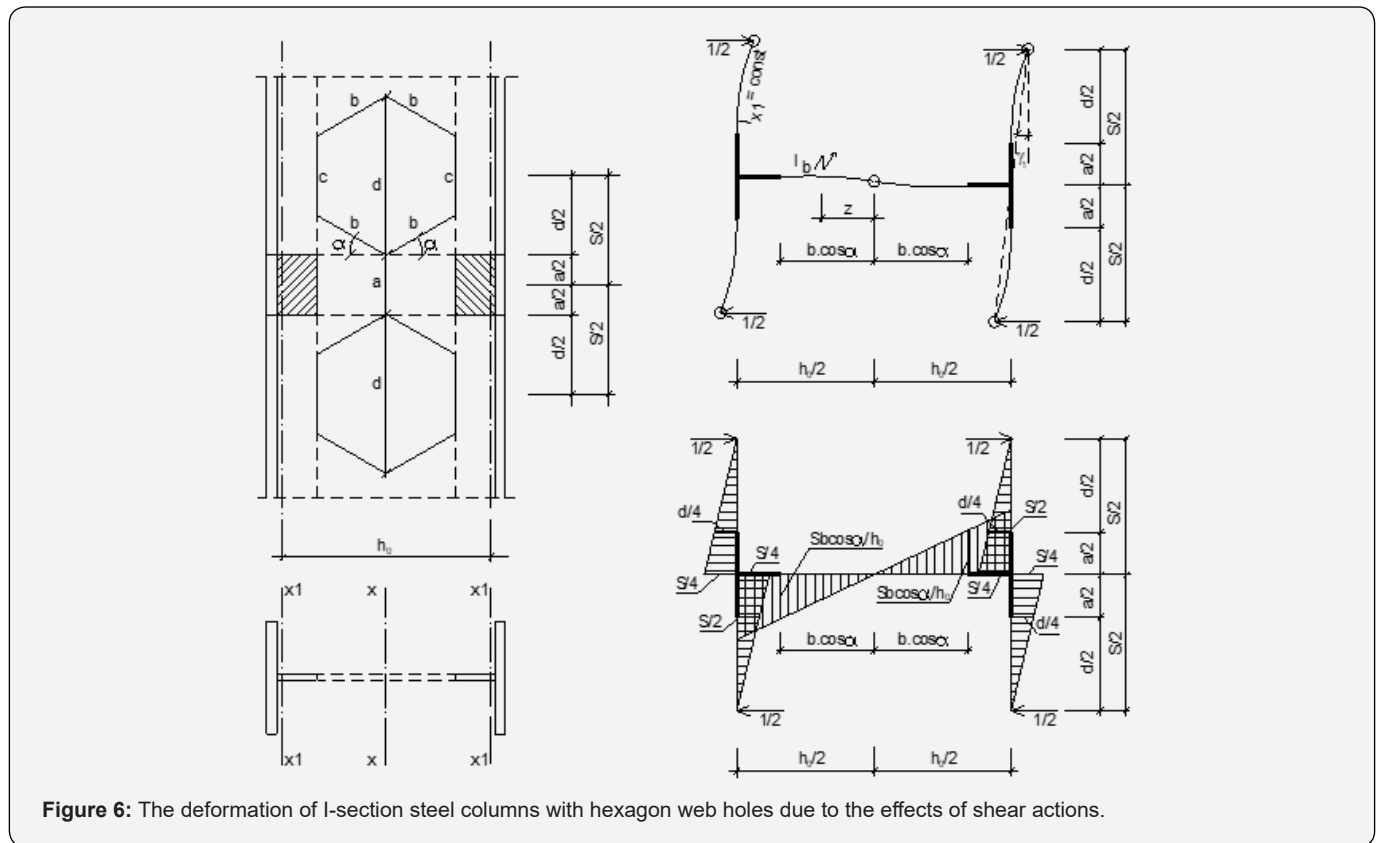


Figure 6: The deformation of I-section steel columns with hexagon web holes due to the effects of shear actions.

where $X = -\frac{3b^2 \cos^2 \alpha}{\operatorname{tg} \alpha (a+2b \sin \alpha)^2} - \frac{3b \cos \alpha}{\operatorname{tg}^2 \alpha (a+2b \sin \alpha)} + \frac{3 \ln(a+2b \sin \alpha) - 3 \ln a}{2 \operatorname{tg}^3 \alpha}$

Put $n = \frac{I_{x1} S^2}{d^3 t_w h_0^2} X$ is the ratio depending on the rigidity of each tee column branch and the dimension of the web holes.

Based on deformations due to the impacts of shear forces, the slippery angle γ_1 can be determined as follows:

$$\Rightarrow \tilde{a}_1 \approx \frac{\ddot{A}}{S} = \frac{d^3(1+n)}{24SEI_{x1}} = \frac{d^3(1+n)}{24SEi_{x1}^2 A_1} = \frac{\ddot{e}_1^2(1+n)}{12EA_{nx}} \cdot \frac{d}{S}$$

where:

$A_{nx} = 2A_1$ - the actual area of two tee branch sections through the centroid of holes;

A_1 - the actual area of one tee branch of the column;

I_{x1} - the moment of inertia of one tee branch of the I-section column about the virtual axis (x_1-x_1);

i_{x1} - the radius of inertia of a tee branch of the I-section

column, $i_{x1} = \sqrt{\frac{I_{x1}}{A_1}}$;

\ddot{e}_1 - the slenderness of one tee brach of the column,

$\ddot{e}_1 = \frac{d}{i_{x1}}$;

S - the distance between two holes;

Therefore, the effective length can be determined as follows:

$$i_t = \sqrt{1 + \frac{\tilde{a}_1 \cdot \delta^2 \cdot E \cdot A_{nx}}{\ddot{e}_x^2}} = \sqrt{1 + \frac{\ddot{e}_1^2(1+n)}{12EA_{nx}} \cdot \frac{d}{S} \cdot \frac{\delta^2 \cdot E \cdot A_{nx}}{\ddot{e}_x^2}}$$

$$i_t = \sqrt{1 + 0,82 \cdot (1+n) \cdot \frac{\ddot{e}_1^2}{\ddot{e}_x^2} \cdot \frac{d}{S}}$$

In general, the equivalent slenderness can be determined as

follows: $\ddot{e}_0 = i_t \cdot \ddot{e}_x = \sqrt{\ddot{e}_x^2 + 0,82 \cdot (1+n) \cdot \frac{d}{S}} \cdot \ddot{e}_x^2$ (6)

The equivalent slenderness of cellular columns depends on:

The slenderness of each tee branch: $\ddot{e}_1 = d / i_{x1}$; The ratio "n" related to the hole dimensions. Therefore, elastic buckling loads N_{cr} of I-section steel columns with a variety of web hole shapes can be presented in Eq. (7) as follows:

$$N_{cr} = \frac{\delta^2 \cdot E \cdot A_{nx}}{\ddot{e}_0^2} = \frac{\delta^2 \cdot E \cdot A_{nx}}{\ddot{e}_x^2 + 0,82 \cdot (1+n) \cdot \frac{d}{S} \cdot \ddot{e}_1^2} \quad (7)$$

It was found that the elastic buckling loads of I-section steel columns with perforations can be calculated on the basis of the dimensions and the shapes of web holes, and the distances between holes.

Conclusion

The paper presents the behaviors of I-section steel columns with perforations according to two axes including the actual axis (y-y) and the virtual axis (x-x). It was found that the behaviour of the I-section steel columns about the actual axis can be considered as a separate working of two tee solid columns whereas these two branches were connected to work together due to the connected webs. Several remarks are given as follows: 1) The effects of shear actions should be accounted for in the determination of elastic buckling loads of I-section steel columns with perforations about the virtual axis; 2) The values of elastic buckling loads depended on the hole dimensions, hole shapes and distance between holes.

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