

Buckling Analysis of Guyed Laminated Wood Transmission Poles



Sriram Kalaga^{1*}, Prema Kumar WP², Supreeth AR³ and Mahendra Kumar P⁴

¹ Professor, Consulting Structural Engineer, USA

² Professor School of Civil Engineering, Reva University, India

³ Department of Civil Engineering, Global Academy of Technology, India

⁴ Royota Engineering, Pvt Ltd., India

Submission: April 19, 2019; Published: May 10, 2019

*Corresponding author: Sriram Kalaga, Consulting Structural Engineer, Glen Burnie, Maryland 21060, USA

Abstract

The buckling loads of guyed laminated wood transmission poles of various heights and classes are computed using the Gere and Carter Method (GCM) and Linear Buckling Analysis using ANSYS finite element software. Four (4) specific end conditions are investigated: fixed-free, fixed-pinned, pinned-pinned and fixed-fixed ends. The buckling loads obtained by the two methods are compared. It is observed that there is good agreement between the values for buckling loads obtained by two approaches for all the end conditions, the maximum average discrepancy being about 2.52%. Suggestions for further extension of the study are made.

Keywords: Buckling; Convergence; End Conditions; Finite Element; Guyed, Pole; Transmission; Laminated; Wood

Notation: d =diameter; d_a =diameter at point of guy attachment; d_g =diameter at ground line; d_e =diameter at pole butt; k =effective length factor; D_e =depth of embedment; E =modulus of elasticity; GD =transverse GL depth; I =moment of inertia; I_A =moment of inertia at A; L =length of pole or column; LW =longitudinal width; L_{AG} =height of pole above ground; M_x =Ultimate GL longitudinal moment; M_y =Ultimate GL transverse moment; P^* =multiplier in Equation (2); P_A =critical load for a uniform column of diameter d ; P_{cr} =critical buckling load; P_E =Euler buckling load; P_x =lateral load 2 feet from pole tip, X-direction; P_y =lateral load 2 feet from pole tip, Y-direction; TD =transverse top depth; α =exponent in Equation (3)

Introduction

Guyed transmission poles are commonly used in transmission lines at turning angle locations and at dead ends (See Figure 1). Although guying is routinely employed in wood pole systems owing to a lack of bending strength of wood, it is also occasionally used for poles of other materials too such as steel, concrete, laminated wood and composite or FRP [1]. As can be seen from Figure 1a-d, the purpose of the guy wires is to back up the wire tension resultants from the conductors and the ground wires and transmit them to the anchors. Figure 1a shows a single anchor associated with all four guy wires; but Figure 1b,c show multiple anchors. Bending moments in the pole are generally minimal since each guy location acts as a partial lateral support, restraining movement in a specific direction. A single set of guy wires can be adequate for small line angles depending on the imposed wire tensions. But a 90-degree dead end shown in Figure 1d requires guys and anchors in both orthogonal directions. The most common slope for a guy wire is 45 degrees. One result

of the guy wire tensions is the vertical load component at each guy location and this component – cumulative for multiple guy wires – acts as an axial load on the pole/ column. For 90-degree dead ends the axial loads come from both directions. Therefore, design involves check for pole buckling [2].

From analysis perspectives, a transmission pole is basically a tapered beam-column with constantly varying cross section from base to top. Design of guyed laminated wood poles in USA is governed by various codes, standards and guidebooks [3-11]. Since wood is a bio-degradable material, general maintenance includes protective treatments [12-15]. Presence in defects within wood (knots, decay) necessitates imposition of a strength reduction factor in design, varying from 0.5 to 0.65, depending on the statistical variability of loads. Past research included several landmark studies on guyed wood poles, including the FE method. Non-linear stiffness matrices were developed for various shapes; but little effort was made to systematically

analyses guyed poles of different structural materials. In addition to wood, guyed poles currently include tubular steel, pre-stressed concrete, laminated wood and fiber-reinforced

polymer (composite) poles. This study is part of an undertaking towards that larger goal which comprises several papers on guyed transmission poles.

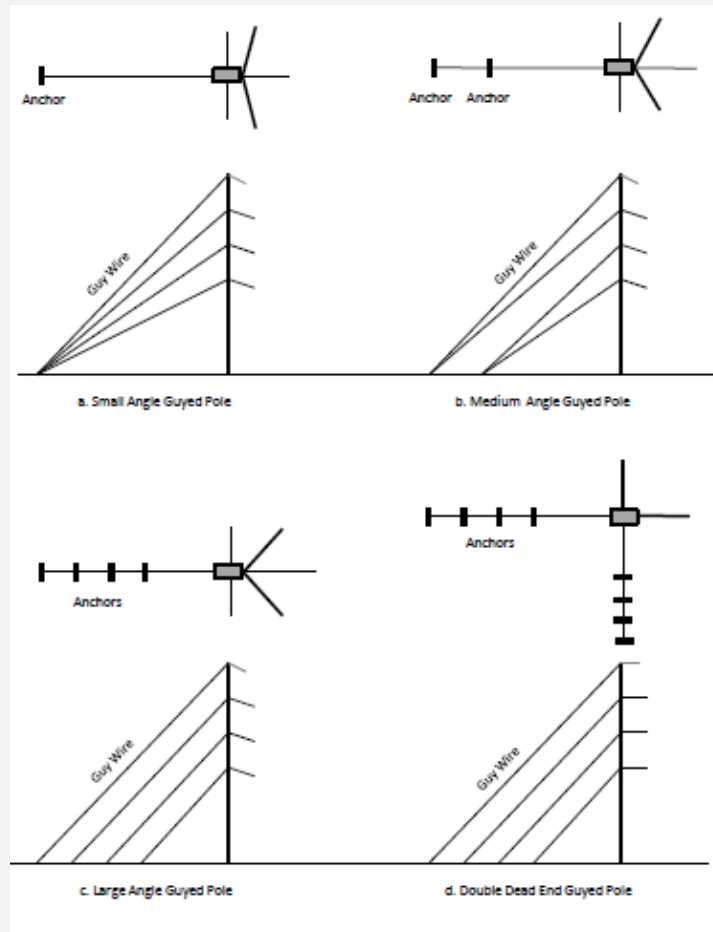


Figure 1a-d: Guyed Transmission Pole Structures - Angle and Dead End.

The aim of this paper is to investigate the buckling behaviour of guyed laminated wood transmission poles employing the FEM and verify the values of the buckling loads with theoretical estimates. A set of 17 laminated wood poles representing the most common sizes and classes of poles utilized in guying situations, together with four kinds of end conditions, were considered. Only linear elastic buckling is studied. Although initial out-of-straightness is often important in buckling patterns, it is not considered here [16]. This paper is intended to be the fourth of a series of papers on guyed poles; others will be on wood, steel, pre-stressed concrete and composite poles.

Literature Review

Theoretically, a transmission pole of any material is a tapered beam-column with constantly varying cross section from base to top. As such, analytical modelling involves the challenge of incorporating stiffness matrices into analysis algorithms. A significant amount of work had been directed therefore towards formulating finite element stiffness matrices to handle tapered

beam-columns [17-24]. The earliest study on tapered beam-columns is contained in the classic 1968 paper by Gere & Cater [25] where expressions were derived for the buckling strength of various steel beam-columns for different end conditions. This study provided the foundation for estimating the buckling capacity of wood poles.

Peabody & Wekezer [26] investigated the buckling strength of transmission and distribution poles using the FEM. Buckling capacities were determined with an Eigenvalue approach using elastic and geometric stiffness matrices of beam elements. One important conclusion drawn in this study is that assuming the unbraced length of the beam-column as the distance from the lowest guy to the ground can lead to a dangerous overestimation of the buckling strength. This implies that a more rational approach would be to consider the entire pole above the ground as a candidate for buckling.

The ASCE Manual 91 [4] is another design reference for guyed transmission structures. This Manual also refers to the Gere-

Carter Method and discusses the difficulties associated with real-life boundary conditions. Idealized end conditions rarely exist in real poles. An important point made in the Manual is that most theoretical methods, including the Gere-Carter Method, lead to large errors in situations where the capacity of the pole is controlled by bending stresses amplified by large compressive loads (i.e.) a true nonlinear beam-column behaviour. Based on a nonlinear finite element analysis of a guyed pole, including guy wires modelled as cable elements, it is shown that theoretical estimates are 1/2 to 2 1/2 times that predicted by the FEM. It is therefore left to the design engineer to adopt a reasonable factor of safety in using theoretical procedures.

The RUS Bulletin 153 [5] also contains another procedure to compute elastic buckling loads of wood poles. It is based on the American Institute of Timber Construction (AITC) approach which suggests that the critical section for a guyed wood pole is located at 2/3 the distance of from the ground to the bottom-most guy attachment. It also recommends a minimum factor of safety of 1.50 to be applied to the computed loads. Subsequent studies suggested that the RUS procedure is more conservative

than the Gere-Carter Method (GCM). Commercial computer programs such as PLS-Pole [27] include both the GCM and RUS options for users. Despite a number of theoretical and analytical investigations, no full-scale tests were performed to confirm and generalize the observations from those studies.

End Conditions of Guyed Poles

IEEE 751 [8] discusses the issue in detail. The end restraints in guyed poles are difficult to evaluate. Poles with bi-sector guys, as seen in Figure 1a-c, approximate a condition of being pinned at the point of guy attachment and fixed at the base, *in plane of the guy wire*. However, at 90 degrees to this plane, the pole is basically a free cantilever. Also, it is generally believed that the conductors also offer some kind of restraint. Therefore, the overall effective boundary conditions may be between the fixed-free ($k=2$) and fixed-pinned ($k=0.7$). For 90 degree guyed dead ends as shown in Figure 1d, the fixed-pinned condition occurs in both planes ($k=0.7$). Some engineers question whether the guy wires restrain lateral motion sufficiently to justify a $k=0.7$. Due to this, routine designs assume $k=1$. (See Figure (1e) for configuration of various boundary conditions).

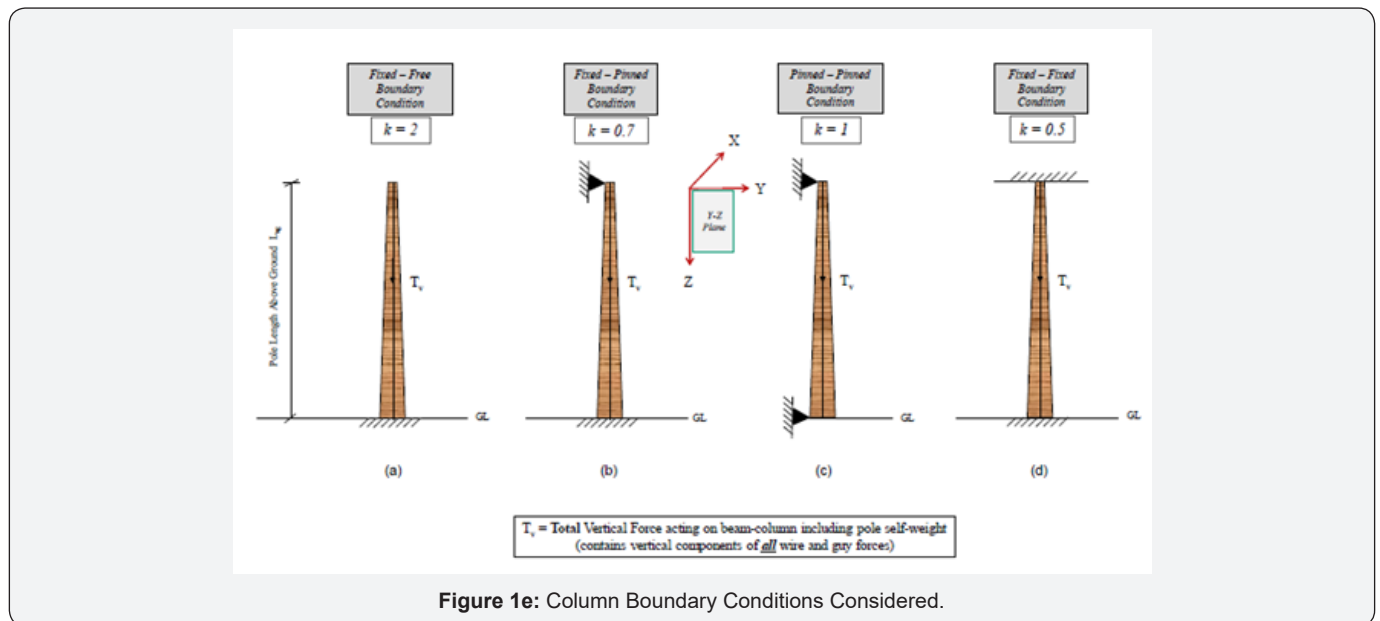


Figure 1e: Column Boundary Conditions Considered.

Euler's Elastic Buckling Theory

A column is considered stable only if the critical elastic buckling load (or Euler load) is not exceeded. The elastic buckling load of a column is defined as the axial load that is just sufficient to keep an initially straight, perfectly elastic bar in a slightly bent form. This load is usually taken as the ultimate load that the column can support, assuming the column is relatively slender and buckling occurs in the elastic range. The Euler's critical buckling load for long slender columns of uniform section is given by:

$$P_E = \frac{\pi^2 EI}{(kL)^2} \quad (1)$$

where

P_E = critical buckling load

k = effective length factor

L = actual length of column

E = modulus of elasticity of column material

I = least moment of inertia of the column cross-section

Equation (1) is obviously applicable only to uniform, homogenous columns where the axial load is concentrically applied at the end of the column. This assumption is not valid for a guyed tapered wood pole: constantly varying cross section aside, a typical wood pole has internal imperfections and axial

loads from guy wires are applied intermittently at various heights along the pole. Hence Euler theory cannot be directly used for such poles.

Gere and Carter Method

The Gere and Carter Method (GCM) [6] is commonly used in practice for calculating critical buckling loads for guyed tapered wood poles. This method proposes modification to the Euler’s critical buckling equation as follows:

$$P_{cr} = P_A P^* \tag{2}$$

where:

P_A = Critical load for a uniform column with circular sections having diameter d (at guy attachment)

P^* = A multiplier dependent on the end conditions of the column

$$= \left\{ \frac{d_g}{d_a} \right\}^\alpha \tag{3}$$

where

α = An exponent that is a function of shape of the column

d_a = Diameter at point of guy attachment

d_g = Diameter at the ground line

L =Distance from ground line to the point of guy attachment

Equations for P_A and P^* for various end conditions [8] are summarized in Table 1.

Table 1: Equations for various end conditions for a tapered pole.

End Conditions	PA	P*
Fixed-Free	$\frac{\pi^2 EI_A}{(2.0L)^2}$	$\left\{ \frac{d_g}{d_a} \right\}^{2.7}$
Fixed-Pinned	$\frac{\pi^2 EI_A}{(0.7L)^2}$	$\left\{ \frac{d_g}{d_a} \right\}^{2.0}$
Pinned-Pinned	$\frac{\pi^2 EI_A}{(1.0L)^2}$	$\left\{ \frac{d_g}{d_a} \right\}^{2.0}$
Fixed - Fixed	$\frac{\pi^2 EI_A}{(0.5L)^2}$	$\left\{ \frac{d_g}{d_a} \right\}^{2.0}$

(Ref: IEEE 751)

The Gere and Carter Method assumed that the column is initially perfectly straight, elastic and compressed by an axial load. It is a theoretical method verified by limited tests on steel shapes for tapered poles of various open and closed cross sections subject to only axial load. When using this method for NESC ice and wind loads with specific load factors, it is recommended to use a factor of safety between 2.50 and 3.0 [20]. For extreme wind loads, where all load factors are 1.0, the resulting factors

of safety will be between 1.5 and 2.0. For pure dead ends, higher safety factors must be used due to larger axial loads.

Application to Selected Laminated Wood Poles

As opposed to round wood poles where the cross section is solid and round, all laminated wood poles are solid but rectangular in cross section. Each lamina is about 1 inch thick (25mm). The cross section is larger at the bottom and tapers to a smaller size at the top. As shown in Figure 2, it has properties about both the orthogonal X and Y axes. The depth of the section LW is constant but the width varies from GD at the bottom to TD at the top.

Five (5) laminated wood poles ranging in length from 50ft. to 70ft. (15.2m to 21.3m), involving four (4) pole classes and four (4) specific boundary conditions are studied. This set of 17 poles of Southern Pine material represent the most common sizes of poles utilized in guying situations. The definition of a pole class is illustrated in Figure 2 while Table 2 shows the numerical values of lateral loads associated with laminated wood pole classes [9,10]. Other design properties of these poles are shown in Table 3. Note that 4 pole classes are considered for 50ft. and 55ft. poles while 3 pole classes were considered for 60ft., 65ft. and 70ft. poles. The values of the critical buckling load obtained by the Gere and Carter Method are given in Table 4. These values are computed using a custom spreadsheet developed for the purpose. In all cases, the effective length for buckling is taken as the pole height above ground LAG.

Table 2: Wood Pole Classes*.

LAM Wood Pole Class Designation *	Longitudinal Strength Lateral Load P_y (lbs.) **	Transverse Strength Lateral Load P_x (lbs.) **
PEL-1-50	2950	4960
PEL-2-50	2820	4550
PEL-3-50	2465	3470
PEL-4-50	2305	3030
PEL-1-55	2870	5220
PEL-2-55	2550	4120
PEL-3-55	2435	3760
PEL-4-55	2290	3325
PEL-1-60	3660	5315
PEL-2-60	2515	4410
PEL-3-60	2350	3860
PEL-1-65	3360	4890
PEL-2-65	3150	4285
PEL-3-65	2160	3550
PEL-1-70	3345	5220
PEL-2-70	2910	3970
PEL-3-70	2000	3290

1ft.=30.48cm, 1lb.=4.45N

* LWS, Inc. ** Applied 2ft from the tip of the pole (rounded to the nearest 5 lbs.)

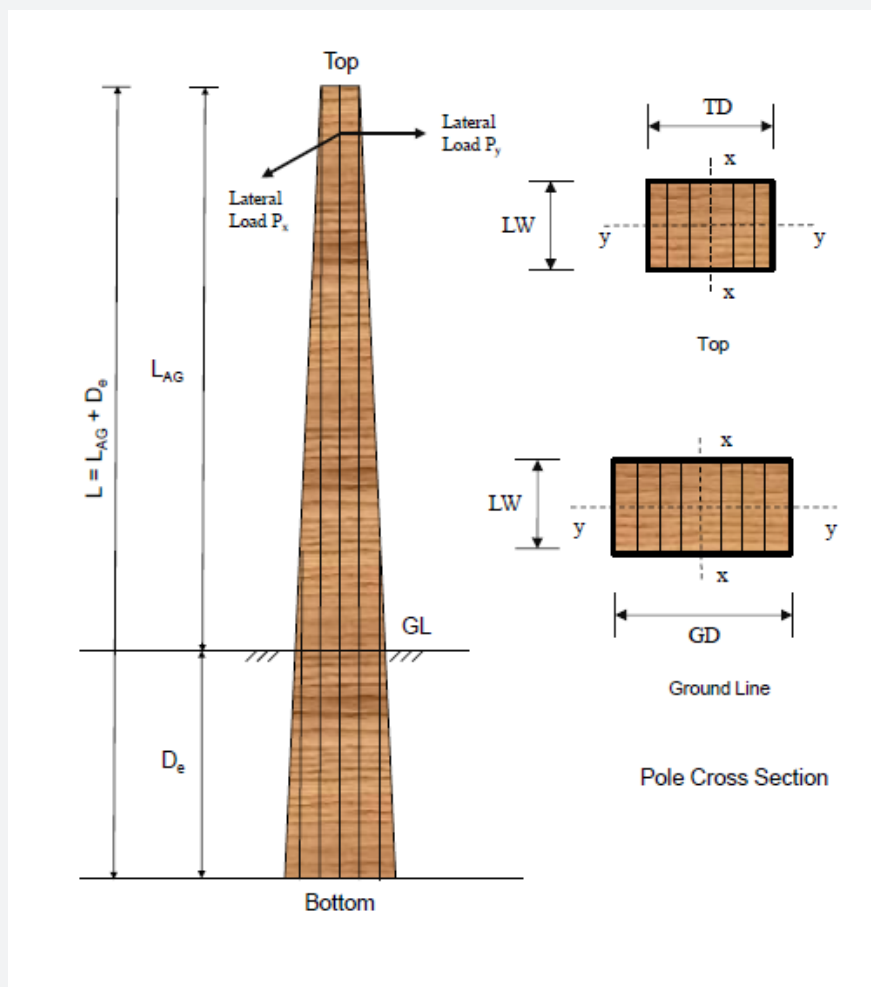


Figure 2: Definition of Laminated Wood Pole Class.

Table 3: Properties of Laminated Wood Poles: LWS Classes.

Pole Length, L (ft)	Pole Class	Ground Line or Embedment D_e (ft)	Pole Height Above Ground, $L_{AG} = L - D_e$ (ft)	Longitudinal Width LW (in.)	Transverse Depth TD at Top (in.)	Transverse Ground Line Depth GD (in.)	Ultimate GL Longitudinal Moment M_x (kip-ft)	Ultimate GL Transverse Moment M_y (kip-ft)
50	PEL-1-50	7	43	8.50	7.00	15.06	120.9	203.5
50	PEL-2-50	7	43	8.50	6.25	14.42	115.7	186.5
50	PEL-3-50	7	43	8.50	5.5	12.6	101.1	142.3
50	PEL-4-50	7	43	8.50	5.00	11.77	94.5	124.3
55	PEL-1-55	7.5	47.5	8.50	7.00	16.28	130.7	237.5
55	PEL-2-55	7.5	47.5	8.50	6.25	14.45	116.0	187.4
55	PEL-3-55	7.5	47.5	8.50	5.50	13.81	110.8	171.1
55	PEL-4-55	7.5	47.5	8.50	5.00	12.99	104.2	151.3
60	PEL-1-60	8	52	10.25	6.25	16.21	182.9	265.8
60	PEL-2-60	8	52	8.50	6.25	15.68	125.8	220.4
60	PEL-3-60	8	52	8.50	6.00	15.64	117.7	193.0

65	PEL-1-65	8.5	56.5	10.25	6.25	15.70	183.3	266.7
65	PEL-2-65	8.5	56.5	10.25	6.00	14.69	171.5	233.5
65	PEL-3-65	8.5	56.5	8.50	6.00	14.69	117.9	193.6
70	EL-1-70	9	61	10.25	6.25	16.93	197.5	308.1
70	EL-2-70	9	61	10.25	6.00	14.71	171.7	234.2
70	EL-3-70	9	61	8.50	6.00	14.71	118.1	194.2

Note: 1. Pole Embedment D_e is equal to 10% of Pole Length +2.0ft. 1in.=25.4mm, 1ft.=0.305m, 1kip-ft=1.356kN-m 1psi=6.895kPa

2. Pole material is SP (Southern Pine) GL=Ground Line

3. Designated Bending Stress $F_{bxx}=2100$ psi; Load \perp to Face of Laminae

4. Designated Bending Stress $F_{byy}=2000$ psi; Load \parallel to Face of Laminae

5. Designated Compressive Stress $F_c = 2200$ psi (Parallel to Grain) Y=Minor axis X=Major axis

6. Designated Shear Stress $F_v = 175$ psi

7. Modulus of Elasticity $E=1.87 \times 10^6$ psi

Table 4: Failure Loads by Gere-Carter Method (kips).

Pole No	Pole Length, $L_{AG}/L^*(ft.)$	Pole Class	Fixed-Free	Fixed-Pinned	Pinned-Pinned	Fixed-Fixed
1	43/50	PEL-1-50	10.6	79.0	39.2	154.9
2		PEL-2-50	10.1	73.7	36.3	143.6
3		PEL-3-50	8.9	63.3	32.0	207.5
4		PEL-4-50	8.4	59	29.1	117.0
5	47.5/55	PEL-1-55	9.3	67.7	33.4	131.8
6		PEL-2-55	8.3	60.4	29.8	117.7
7		PEL-3-55	7.8	55.1	27.2	109.3
8		PEL-4-55	7.3	51.9	25.6	101.1
9	52/60	PEL-1-60	13.3	94.9	46.8	185.0
10		PEL-2-60	7.3	52.3	25.8	103.7
11		PEL-3-60	7.3	52.0	25.6	101.3
12	56.5/65	PEL-1-65	10.9	77.6	38.3	154
13		PEL-2-65	10.5	74.5	36.1	145.2
14		PEL-3-65	6.0	42.5	20.6	82.8
15	61/70	PEL-1-70	9.9	70.1	34.6	136.7
16		PEL-2-70	9.0	63.9	31.0	124.6
17		PEL-3-70	5.1	36.5	17.7	71.0

* See Figure 2 and Table 3 for definition for L_{AG} .

1ft.=0.3048m, 1kip = 4.45kN

Buckling Analysis using FEM

In the present study, ANSYS software [28] is used to perform linear or classical finite element buckling analysis of tapered wood poles. The finite element used is a Beam-188 element that has two end nodes with 3 translational and 3 rotational degrees of freedom at each node. This element is based on Timoshen-

ko beam theory, includes shear deformation effects, well-suited for both linear/non-linear applications and flexural, lateral and torsional stability (using Eigenvalue buckling) problems. All FE models are planar beam-columns in the Y-Z plane (Major-axis bending) with movement out-of-plane restrained (see Figure 1e).

Convergence study

A convergence study was made to determine the number of elements which yields accurate result. A tapered laminated wood pole was discretized using uniform two-node Beam 188 elements. The results are provided in Table 5 for fixed-free end

conditions, indicating that 12 elements would give sufficiently accurate result for buckling load. Hence, in all further work in this paper, a finite element model having 12 elements is used. (In comparison, Peabody and Wekezer used 14 equal length beam elements in their FE studies).

Table 5: Results of convergence study.

No.	No. of Elements	Critical Load (kips)
1	1	9.775
2	2	10.662
3	3	10.838
4	4	10.898
5	5	10.926
6	6	10.94
7	7	10.949
8	8	10.955
9	9	10.959
10	10	10.961
11	11	10.964
12	12	10.965

Note: 50ft. PEL-1-50 Pole

$L_{AG} = 43\text{ft. (13.11m)}$

Longitudinal Width LW = 8.5in. (21.59cm)

Transverse Depth TD at Top=7.00in. (17.78cm)

Transverse Depth GD at Ground line =15.06in. (38.25cm)

$E = 1.87 \times 10^6 \text{psi (12.88} \times 10^6 \text{kPa)}$

1inch=2.54cm, 1ft.=0.3048m, 1kip=4.45kN, 1psi=6.89kPa

Buckling loads from FEM

The adopted FE idealization is shown in Figure 3. To maintain consistency with the GCM, the effective length of the pole

FE model is taken as the pole height above ground, LAG. Table 6 gives the critical buckling loads obtained by ANSYS for the 17 laminated wood poles.

Table 6: Failure loads by linear buckling analysis (kips).

Pole No	Pole Length, $L_{AG}/L^*(\text{ft.})$	Pole Class	Fixed-Free	Fixed-Pinned	Pinned-Pinned	Fixed-Fixed
1	43/50	PEL-1-50	11	77.2	38.1	150.3
2		PEL-2-50	10.3	71.9	35.6	139.9
3		PEL-3-50	9.1	63.0	31.2	207.5
4		PEL-4-50	8.4	58.3	28.8	113.3
5	47.5/55	PEL-1-55	9.6	66.4	32.8	129.1
6		PEL-2-55	8.5	59.1	29.2	114.9
7		PEL-3-55	8.0	54.7	27.1	106.2
8		PEL-4-55	7.5	50.8	25.2	98.6
9	52/60	PEL-1-60	13.6	92.8	46.0	180.2
10		PEL-2-60	7.6	51.8	25.7	100.7
11		PEL-3-60	7.5	51.0	25.3	99.0
12	56.5/65	PEL-1-65	11.3	77.1	38.2	149.8
13		PEL-2-65	10.6	72.9	36.1	141.6
14		PEL-3-65	6.0	41.5	20.6	80.8

15	61/70	PEL-1-70	10.3	69.4	34.4	134.7
16		PEL-2-70	9.1	62.6	31.0	121.6
17		PEL-3-70	5.2	35.7	17.7	69.4

* See Figure 2 and Table 3 for definition for L_{AG} .

1ft.=0.3048m, 1kip=4.45kN

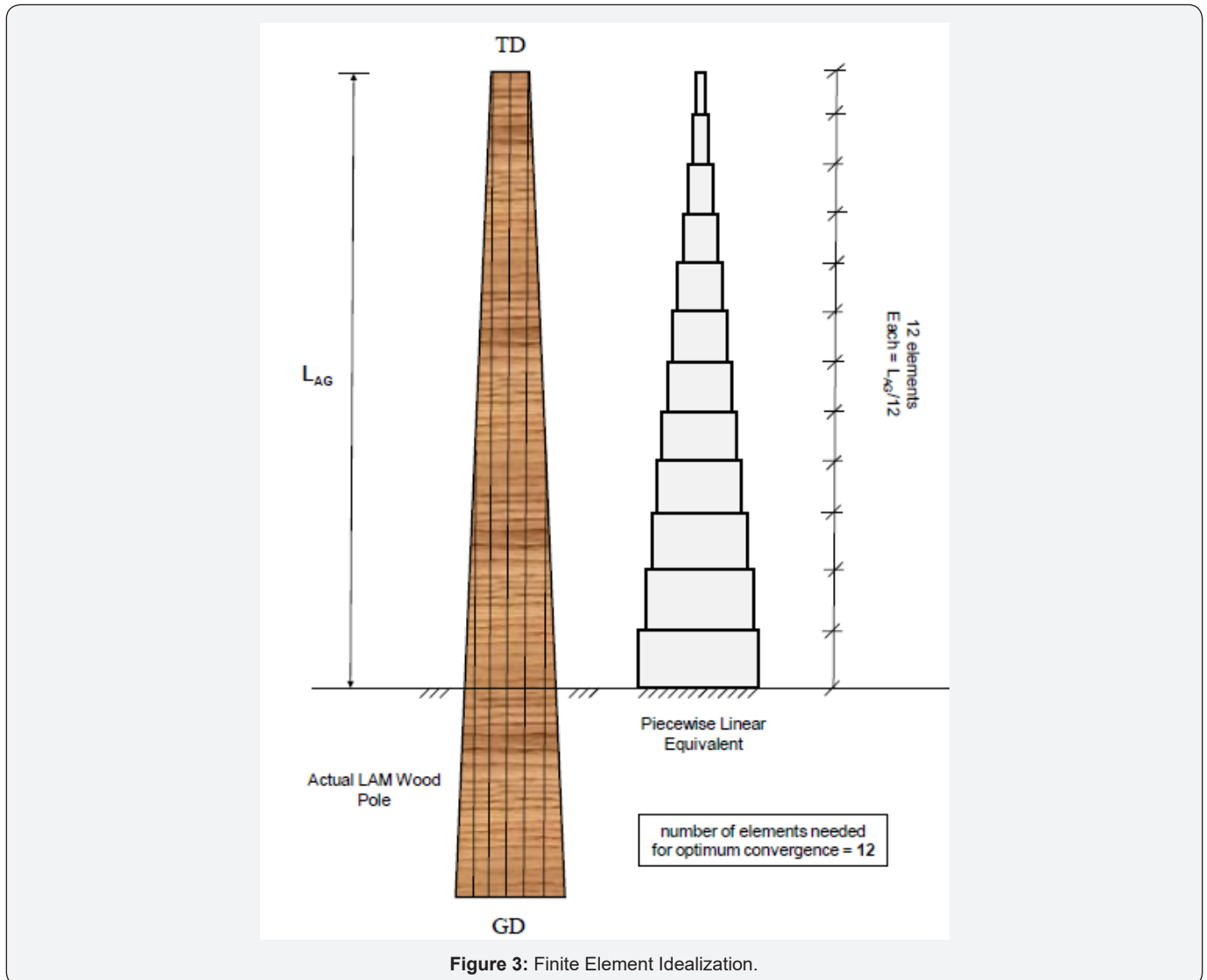


Figure 3: Finite Element Idealization.

Comparison of Results and Discussion

The critical buckling loads obtained by Gere and Carter Method and linear buckling analysis are compared and the computed percentage discrepancy is shown in Table 7. There is excellent agreement between the two sets of values. From the table, it is observed that the discrepancy is minimum in the case of pinned-pinned end condition and maximum for fixed-fixed end condition. The maximum value of percentage discrepancy is +3.34 for the fixed-fixed end condition. The average % discrepancy values for the four boundary conditions investigated were +2.17, -1.70, -1.06 and -2.52, respectively. The main inference

that can be drawn – pending validation with full-scale testing– is that the Gere and Carter Method is adequate for calculating nominal buckling loads, subject to application of factor of safety. Laboratory testing will help establish what rational factors of safety are needed for various loading situations. Peabody & Wekezer [26] obtained similar results for their FE analysis of an 80ft. (24.4m)-long wood pole where they compared FE results with those of Gere and Carter. The % discrepancy values for the same four boundary conditions were +4.43, -1.74, -0.35 and +0.36, respectively. The paper recommended GCM for calculating buckling strength of transmission and distribution poles; but suggested performing a series of full-scale tests to validate GCM.

Table 7: Comparison of Failure Loads (Gere-Carter Method vs Linear Buckling Analysis).

Pole No	Pole Length, LAG/L*(ft.)	Pole Class	Fixed-Free	Fixed-Pinned	Pinned-Pinned	Fixed-Fixed
1	43/50	PEL-1-50	3.34	-2.26	-2.79	-2.94
2		PEL-2-50	2.03	-2.42	-2.15	-2.57
3		PEL-3-50	1.46	-0.4	-2.59	-2.99
4		PEL-4-50	0.38	-1.21	-0.9	-3.19
5	47.5/55	PEL-1-55	2.71	-1.9	-1.63	-2.05
6		PEL-2-55	2.23	-2.25	-1.99	-2.39
7		PEL-3-55	2.98	-0.8	-0.33	-2.81
8		PEL-4-55	2.66	-2.15	-1.58	-2.48
9	52/60	PEL-1-60	2.6	-2.2	-1.62	-2.55
10		PEL-2-60	2.94	-0.82	-0.35	-2.82
11		PEL-3-60	2.96	-1.92	-1.34	-2.24
12	56.5/65	PEL-1-65	3.13	-0.67	-0.19	-2.68
13		PEL-2-65	1.03	-2.25	-0.07	-2.48
14		PEL-3-65	0.97	-2.27	-0.11	-2.48
15	61/70	PEL-1-70	3.21	-1.11	-0.42	-1.51
16		PEL-2-70	1.15	-2.14	0.04	-2.37
17		PEL-3-70	1.1	-2.17	-0.01	-2.37
		Average	+2.17	-1.7	-1.06	-2.52

Upper and Lower Bounds of Buckling Capacities

As stated earlier, it is generally believed that the overall effective boundary conditions for a guyed pole may be between the fixed-free ($k=2$) and fixed-pinned ($k=0.7$). Therefore, these two situations may be treated as lower and lower bounds related to the buckling capacity. It is possible to obtain a mean value in-between the two bounds as a design reference. Figures 4-8

show the buckling capacities bounds—and their mean values – for the 17 poles considered in the study. The values refer to GCM. For example, the mean value of buckling strength for a 60ft. PEL-2-60 pole is 29.8kips (132.6kN). Assuming a factor of safety of 2.0 and extreme wind loads, the allowable buckling load on the pole is $29.8/2=14.9$ kips (66.3kN). This value may be considered as a design reference while checking buckling.

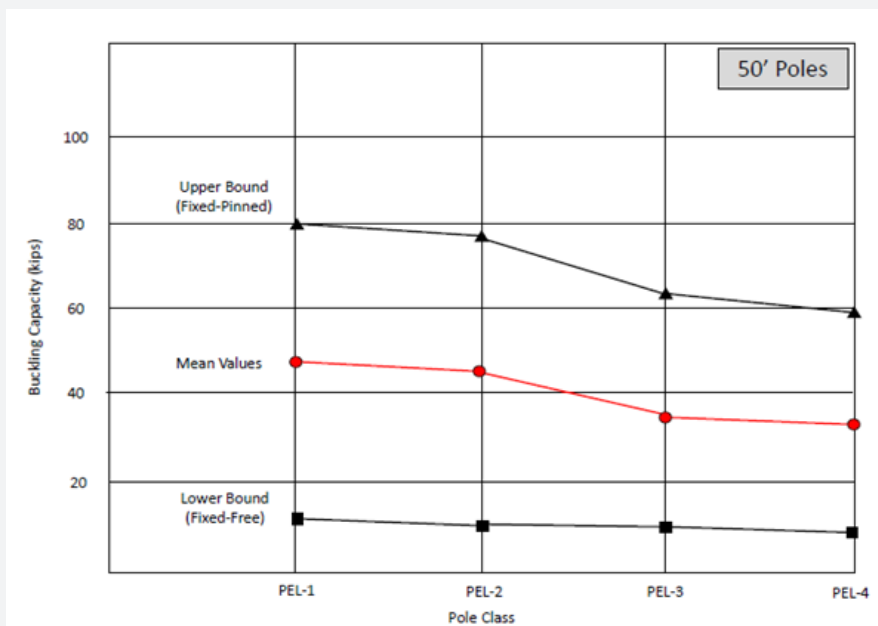


Figure 4: Upper and Lower Bounds of Buckling Capacity.

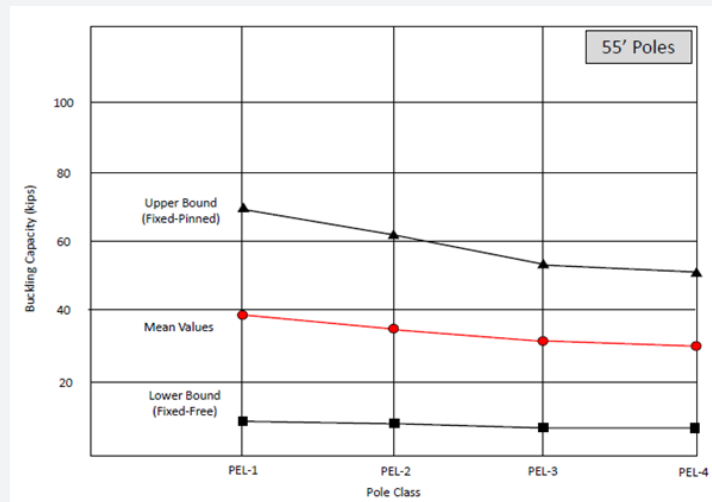


Figure 5: Upper and Lower Bounds of Buckling Capacity.

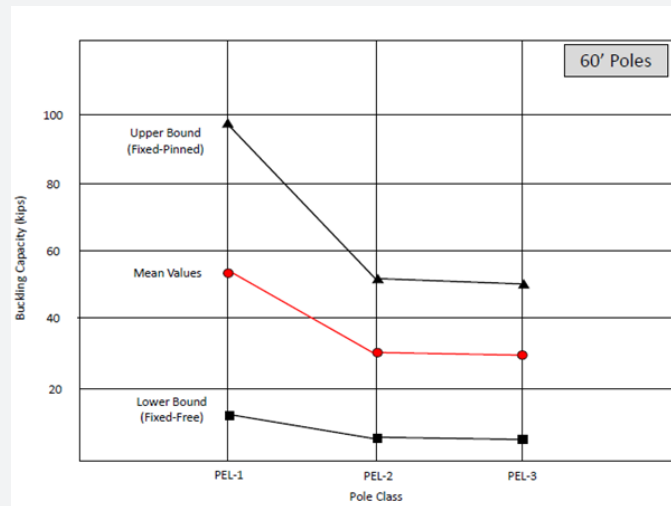


Figure 6: Upper and Lower Bounds of Buckling Capacity.

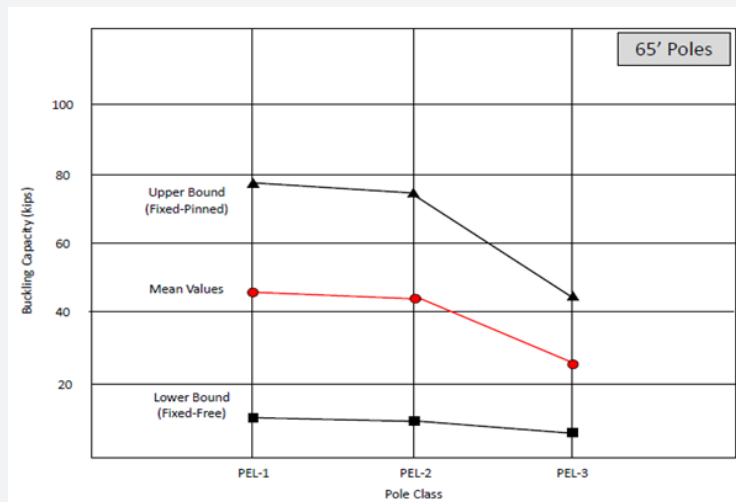


Figure 7: Upper and Lower Bounds of Buckling Capacity.

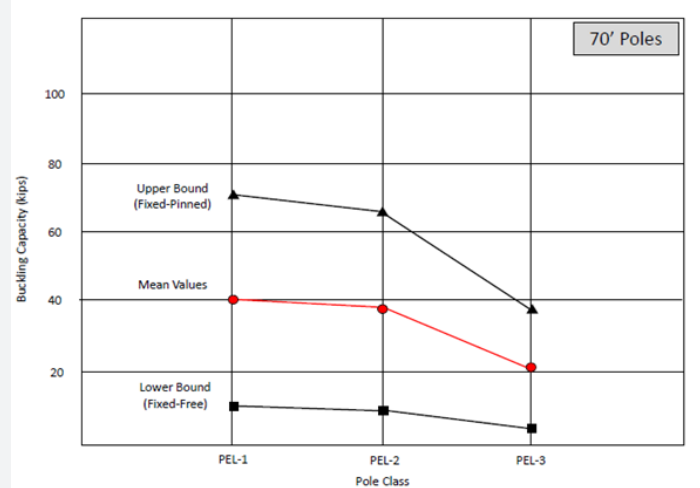


Figure 8: Upper and Lower Bounds of Buckling Capacity.

Conclusion

Seventeen laminated wood poles were analysed by a 12-element advanced FE model to determine critical buckling loads which were compared with theoretical estimates using the well-known Gere and Carter Method. The percentage of discrepancy between the buckling loads given by GCM and FEM is minimum for fixed-fixed end condition and maximum for fixed-free end condition. For all the cases studied in this paper, the maximum % discrepancy is about -2.52. Similar results were obtained by Peabody & Wekezer [26] in their 1994 studies. For the cases considered it is seen that the Gere and Carter Method gives buckling loads that are quite close to that given by FEM and hence may be used conveniently in practice. To assist in routine design, the upper and lower bounds – and their mean value – of the buckling load can be considered. Given the uncertainty associated with correctly modelling the end restraints of a guyed pole, it is suggested that a series of full-scale tests be performed to rationalize on the findings of this and previous studies.

References

- Kalaga S, Yenumula P (2016) Design of Electrical Transmission Lines: Structures and Foundations, (1st edn), CRC Press, Florida, USA, p. 426.
- Bulletin 1724E-200 (2015) Design Manual for High Voltage Transmission Lines. Rural Utilities Services, United States Department of Agriculture USDA.
- ANSI 05.1 (2008) American National Standard for Wood Poles–Specifications and Dimensions. ANSI Standard 05-1-2008, New York, USA.
- ASCE 91 (1997) Design of Guyed Electrical Transmission Structures. ASCE Manual, Reston, Virginia, USA.
- Bulletin 1724E-153 (2003) Electric Distribution Line Guys and Anchors. Rural Utilities Services, United States Department of Agriculture USDA.
- Bulletin 1728F-700 (2017) Specifications for Wood Poles, Stubs and Anchor Logs. Rural Utilities Services, United States Department of Agriculture USDA.
- Bulletin 1724F-702 (2011) Specifications for Quality Control and Inspection of Timber Products. Rural Utilities Services, United States Department of Agriculture USDA.
- IEEE-751 (1991) Trial Use Design Guide for Wood Transmission Structures. Institute of Electrical and Electronics Engineers, New York, New York, USA.
- Laminated Wood Systems (2007) E-LAM Tangent Poles–Southern Pine and Coastal Fir. LWS Catalog, Minneapolis, Minnesota, USA.
- Laminated Wood Systems (2007) Engineered Laminated Wood Utility Structure Design. LWS Seminar, Minneapolis, Minnesota, USA.
- NESC-2012 (2002) National Electrical Safety Code, ANSI C-2. Institute of Electrical and Electronics Engineers, New York, USA.
- AITC Standard 109 (2007) Standard for Preservative Treatment of Structural Glued Laminated Timber. American Institute of Timber Construction, Oregon, USA.
- AITC Standard 110 (2001) Standard Appearance Grades for Structural Glued Laminated Timber. American Institute of Timber Construction, Oregon, USA.
- AITC Standard 111(2005) Recommended Practice for Protection of Structural Glued Laminated Timber during Transit, Storage and Erection. American Institute of Timber Construction, Oregon, USA.
- Forest Products Laboratory (1999) Wood Handbook: Wood as an Engineering Material. Report FPL-GTR-190, Forest Products Laboratory, USDA.
- Savic J (1991) Buckling Behaviour of Wood Poles. MS thesis, University of Manitoba, Canada.
- Ali R (1970) Derivation of Stiffness Matrix for a Tapered Beam Element. Report, Department of Transport Technology, Loughborough University of Technology, UK.
- Aristizabal-Ochoa JD (1987) Tapered Beam and Column Elements in Unbraced Frame Structures. Journal of Computing in Civil Engineering ASCE 1(1): 35-49.
- Ashraf M, Ahmad HM, Siddiqi ZA (2005) A Study of Power Transmission Poles. Asian Journal of Civil Engineering 6(6): 511-532.
- Banerjee JR, Williams FW (1986) Exact Bernoulli-Euler Static Stiffness Matrix for a Range of Tapered Beam-Columns. International Journal of Numerical Methods in Engineering 23: 1615-1628.

21. Chugh AK, Biggers SB (1976) Stiffness Matrix for a Non-Prismatic Beam-Column Element. International Journal for Numerical Methods in Engineering 10: 1125-1142.
22. Costello GA (1967) Stability of Transmission Line Structures. Journal of the Engineering Mechanics Division 93(EM4): 19-29.
23. Li G-Q, Li J-L (2007) Elastic Stiffness Equation for Tapered Beam Element. Advanced Analysis and Design of Steel Frames, Wiley Inter Science, doi.org/10.1002/9780470319949.ch3.
24. Sapalas V, Samofalov M, Saraskinas V (2005) FEM Stability Analysis of Tapered Beam-Columns. Journal of Civil Engineering and Management 11(3): 211-216.
25. Gere JM, Carter WO (1962) Critical Buckling Loads for Tapered Columns. ASCE Journal of the Structural Division 88 (ST1): 1-12.
26. Peabody AB, Wekezer JW (1994) Buckling Strength of Wood Power Poles Using Finite Elements. ASCE Journal of Structural Engineering 120(6): 1893-1908.
27. PLS-POLE™ (2012) Computer Program for the Analysis and Design of Transmission Poles. Power Line Systems, Inc., Madison, Wisconsin, USA.
28. ANSYS (2015) Users' Manual, Ansys Inc. Canonsburg, Pennsylvania, USA.



This work is licensed under Creative Commons Attribution 4.0 License
DOI: [10.19080/CERJ.2019.08.555735](https://doi.org/10.19080/CERJ.2019.08.555735)

**Your next submission with Juniper Publishers
will reach you the below assets**

- Quality Editorial service
- Swift Peer Review
- Reprints availability
- E-prints Service
- Manuscript Podcast for convenient understanding
- Global attainment for your research
- Manuscript accessibility in different formats
(Pdf, E-pub, Full Text, Audio)
- Unceasing customer service

Track the below URL for one-step submission
<https://juniperpublishers.com/online-submission.php>