

Juniper

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Review Article Volume 3 Issue 5 - August 2017 DOI: 10.19080/BBOAJ.2017.03.555621 Biostat Biometrics Open Acc J Copyright © All rights are reserved by Atanu B

Multiple Imputations for Determining an Optimum Biological Dose of a Metronomic Chemotherapy



Atanu B*, Gajendra V2, Jesna J2 and Ramesh V3

*Centre for Cancer Epidemiology, The Advanced Centre for Treatment, Research and Education in Cancer (ACTREC), Tata Memorial Centre, Mumbai, India 2Department of Applied Mathematics, Indian Institute of Technology -Dhanbad- 826004, India.

³King Abdullah International Medical Research Center (KAIMRC), King Saud Bin Abdulaziz University for Health Sciences, Ministry of National Guard-Health Affairs, Riyadh, Kingdom of Saudi Arabia.

Submission: August 23, 2017; Published: October 24, 2017

*Corresponding author: Atanu Bhattacharjee, Department of Statistics, Gauhati University, Guwahati, India; Email: atanustat@gmail.com

Abstract

The doses of chemotherapy selected in clinical practice are routinely obtained by the Maximum Tolerated Dose (MTD) approaches. It is believed that an increase in dose will lead to an increase in tumor response. The effect on angiogenesis is achieved by targeting Circulating Endothelial Cell(CEC). The effect on CEC is restricted to an antiangiogenic window in tumor cell line studies The challenge is to establish the optimal biological dose (OBD) of MC which would have maximized inhibiting effect on CEC. The inhibiting effect of CEC is required to measure with repeated manners and can be considered as Surrogate Marker of Angiogenesis. There is no consensus on the most appropriate approach to surrogate marker response with effective metronomic chemotherapy. Therefore a simulation study was performed to assess the OBD on the performance of MC. Datasets were generated to resemble the skewed distributions seen in a motivating head and neck cancer (HNC) example. The CEC count is considered as the time-dependent surrogate marker. The joint distribution of the time-to-event and longitudinal outcomes are considered. The missing data mechanism is defined through consideration of the conditional distribution of the time-to-dropout condition to the complete vector of longitudinal outcomes. The parameters of interest are estimated through the Bayesian approach on joint modeling.

Keywords: MTD; CEC; OBD; Missing; Joint Modeling; Time=to-Event

Introduction

The doses of chemotherapy selected in clinical practice are routinely obtained by the Maximum Tolerated Dose (MTD) approaches. It is believed that an increase in dose will lead to an increase in tumor response. The dose selected for phase 2 and further studies is one dose level below the MTD level in Phase I studies [1-3]. However, this conventional dosing of chemotherapy has routinely compromised the QOL of patients and may lead to a selection of chemo-resistant clones [4-6]. The Metronomic Chemotherapy (MC) has been suggested as an alternative strategy to overcome such effects. The strategy in MC is to administer subtoxic doses (i.e.nearly of MTD) of same chemotherapy drugs for long periods to target angiogenesis [7-10]. The effect on angiogenesis is achieved by targeting Circulating Endothelial Cell(CEC). The effect on CEC is restricted to an antiangiogenic window in tumor cell line studies [1,11,12].

In tumor cell line studies a drug would start exerting an antiangiogenic effect at a low dose level and it would continue to exert it till an upper dose level. Drug levels below the lower dose level and above the upper dose level won't exert an antiangiogenic effect. The challenge is to establish the optimal biological dose (OBD) of MC which would have maximized inhibiting effect on CEC. The inhibiting effect of CEC is required to measure with

repeated manners and can be considered as Surrogate Marker of Angiogenesis [13]. The failure to achieve an inhibiting effect of CEC proceeds to the recurrence of tumor and further death to a patient. The bridged problems are the determination of OBD of MC through consideration of repeatedly measured CEC maker's values on time-to-event data. However, in this paper, we will concentrate on reasonably two best performing OBD and their effectiveness to maintain continuously measured CEC maker's values on angiogenesis and the further time-to-event rate among the treated patients with specific MC dose.

Methods

The simulation techniques adopted within this study are given below. All simulations were carried through the freely available R statistical software, thus allowing all researchers access to any suitable methods identified.

Generating the datasets

There is no consensus on the most appropriate approach to surrogate marker response with effective metronomic chemotherapy. Therefore a simulation study was performed to assess the OBD on the performance of a MC. Datasets were generated to resemble the skewed distributions seen in a motivating head and neck cancer (HNC) example. The CEC count is considered as time dependent surrogate marker. The

baseline CEC count in the blood of HNC patients incorporated from normal distribution (with mean 114 CEC per ml; SD 15) for a total of 220 patients. The dose 1 and dose 2 are considered as OBD in this work with simplicity [14]. However, it is possible to consider several doses and obtain the best performing optimum dose based on the controlled level of surrogate marker i.e. CEC. The ID's of 200 patients were randomly assigned to the dose 1 and dose 2 with metronomic chemotherapy from the binomial distribution. The baseline measurement of four covariates named with ECOG (coded 0 and 1), HB Level(<12 and 12), Tumor size (mean 4:0 cm; SD 2) and Histological grades (well, moderate and poor)were generated randomly for a total of 220 patients and merged with the excel sheet. The ECOG, HB level and Histological grade were generated from binomial and multinomial distribution respectively.

The baseline tumor sizes were obtained through normal distribution. Further, the five follow-up visits observations for CEC and tumor size were assumed to be distributed with the normal distribution. The mean value for CEC at time points t1; t2; t3; t4; t5 were assigned with mean 124,128,135,126,120 respectively. The SD was considered for each time points of CEC values to be generated as random measurements. The tumor size assigned with mean 4:0; 3:4; 3:2; 3:0; 3:2 with SD (2) for the time points t1; t2; t3; t4; and t5 respectively. The continuous covariates were postulated with a linear effect on the log relative hazard. An exponential distribution with a hazard rate of 0.0003 was considered to generate the uncensored survival duration. It is approximated with the hazard rate in the HNC [15]. The censored duration was also generated from the exponential distribution with a hazard rate of 0.0003 with approximately 45% censored observations. The required survival duration was defined for each cases as the minimum of the uncensored and censored survival duration and the event status defined accordingly. The recurrence is considered as event of interest. The survival duration is represented as progression free survival (PFS).

Model

The i^{th} subject's longitudinal measurement at time point t is denoted as $Y_i(t)$. Further, the time to occurrence of event is defined as T_i and C_i respectively. The term T_i and C_i are defined as time to outcome-dependent and outcome-independent dropout respectively. The measured data is defined $Y_{ij} = \left\{Y\left(t_{ij}\right), j=1,.....,n_i\right\}$, as for the specific time point t_{ij} . It is assumed that, $U_i = \min(T_i, C_i)$, the observed event time, and the corresponding event indicator, and the measured observation is defined as $Y_{ij} = \left\{Y\left(t_{ij}\right), j=1,.....,n_i\right\}$, the longitudinal responses at the specific occasions t_{ij} at which measurements were taken. The subject-specific longitudinal trajectories is defined as

$$Y_{ij} = m_i(t) + \epsilon_i(t) \quad (1)$$

$$m_i(t) = x_i'(t)\beta + z_i'(t)b_i \quad (2)$$

$$b_i(t) \sim N(0, D) \epsilon_i \sim N(0, \sigma^2) \quad (3)$$

In equation (2) the term $x_i(t)$ is used as fixed effects for the β and $z_i(t)$ as the random effects $b_i t$. The error terms are time-dependent and assumed that the errors are mutually independent with random effects. The random error is assumed with normally distributed with mean zero and variance σ^2 . Thereafter, we will give emphasize on $m_i(t)$ as a component of $Y_i(t)$. The risk of event is defined as

$$h_i(t|M_i(t),\omega_i) = \lim_{dt\to 0} \Pr\{t \le T < +dt | T_i \ge t, M_i(t)\} / dt$$
 (4)

$$h_i(t|M_i(t)) = h_0(t) \exp\{\gamma'\omega_i + \alpha m_i(t)\}, t > 0, (5)$$

The unobserved longitudinal process up to time point is defined as $M_i(t) = \{m_i(s), 0 \leq s \leq t\}$. The baseline risk function and covariates are defined as $h_0(\cdot)$ and with regression coefficients γ . The parameter α is used to facilitate the effect of the underlying longitudinal outcome on the risk for an event. The relative change in the risk for an event at time t is covered through $\exp(\alpha)$ as one unit increase in $m_i(t)$ at the same time point. It shows that the relative risk for an event at time t depends only on the current value of the time-dependent marker $m_i(t)$. It stands that the survival function depends on the whole longitudinal response history $M_i(t)$, Mi(t),through the relation between the survival function and the cumulative hazard function, i.e.,

$$S_i(t)(t|M_i(t)) = \Pr(T_i > t|M_i(t)) = \exp(-\int_0^t h_0(s) \exp\{\gamma'\omega_i + \alpha m_i(s)\} ds)$$
 (6)

The estimation of $S_i(t)$ is dependent on the estimation of $M_i(t)$. Therefore, it is important to specify the time dependent structure in $x_i(t)$ and $z_i(t)$ can be considered with high-dimensional vector of functions with time t. The splines as a vector of choice is preferred due to their numerical suitability and local nature [16]. The spline based approach is already adopted and found suitable like B-splines with multidimensional random effects [17,18] and cubic splines [19]. The joint model is defined as

$$Y_i(t) = m_i(t) + \epsilon_i(t) \tag{7}$$

It is assumed with $u_i(t)$ is independent with b_i and it follows mean-zero with stochastic process. The error term \in (t), and $m_i(t)$ has the mixed-effects model structure as defined in equation (1) and (2). The latent stationary Gaussian process through shared processes [20] and Ornstein-Uhlenbeck Process [21] on joint modeling have adopted and those approaches found appropriate with different dynamic biological scenario that generated with data. The subject specific trajectory is dedicated through time independent random effects b_i alone. It involves that the shape of the longitudinal pro le of each subject is natural feature of this subject that is constant in time. It is possible to generate indistinguishable fits to the data, if the serial correlation term $u_i(t)$ has not been addressed properly by random-effects structure under the consideration of linear mixed model. However, it is difficult to address random effect and serial correlation simultaneously through a single model. It is easier to consider with random-effects by design matrix z_i . It is natural practice to avoid the consideration of specific

distribution for the function $h_0(\cdot)$ of to withdraw the impact of misspecifying the distribution of survival times. Incase of joint modeling it leads to underestimate of the parameter of interest

[22]. It is required to define $h_0(\cdot)$. It can be linked with risk function corresponding to an know parametric distribution or flexible parametric distribution at baseline risk function [23-25].

The objectives of this study raised the challenges. For instance, the subject with controlled CEC value may have controlled tumor growth, having lesser risk of recurrence and relatively lesser risk of death due to cancer. It can be defined as "nonignorable" missing data [26,27]. The generic attempt is to apply longitudinal data model through consideration of CEC value changes, but it may generate biased estimates. The Cox PH model can be considered to explore the relation between CEC value (i.e. as time-dependent covariate) and time to recurrence or death, when the true CEC trajectory $\overline{Y}_i(T_i)$ value is known to us. There are two more challenges. First, the CEC value is prone to be affected with considerable amount of measurement error due to both biological variability and presences of laboratory. The widely used method is to substitutes the observed timedependent covariate for the true covariate values in the PH model. However, this method can leads to biased estimates of the relative risk parameters and it can leads towards biased estimates of the relative risk parameters on measurement error [28,29]. Secondly, the CEC value observed intermittently, it is not feasible(due to costly procedure) to repeatedly measured at the exact time when failure event occurs for the individual in corresponding risk group. The normal procedure is to consideration of "Last Observation Carry Forward (LOCF)" as

a representative of future CEC value from past measurement. Although it is not robust procedure because time to event and corresponding true CEC value will not be there to be correlated.

The LOCF method fails to consider the measurement error, it also overlooks the possible trend of the CEC, resulting very inferior inputs about missing markers values. It leads to poor estimates of the relative risk of parameters. The measurement error can be handled with smoothing technique. The regression calibration is suitable to capture the available trend of the covariates over time and thereafter impute the missing values of covariates for individuals at risk. The imputed values can be

adopted in the disease risk model if they are fitting $Y_i^*(t)$ at the time of each event. This procedure can be adopted through Cox PH model and mixed effect modeling. However, there are certain chances to get the biased results and the estimates of the risk parameters associated with the longitudinal data may not be true, particularly for the relatively sparse longitudinal data. We tried to attempt with joint modeling framework through consideration of longitudinal and time-to-event data analysis.

The idea is to maximizing the likelihood $\left[T_i,Y_i\middle|M_i\right]$ in terms of covariate process and time-to-event data. The informative drop-out assumed to be adjusted with survival modeling, and thereafter unbiased information about the longitudinal covariates were included into the survival model. It helped us to make joint between the failure time with the longitudinal surogate marker. The joint modeling is attempted to build the robust estimates of the parameter through modeling [27,28].

Joint model

A separate term n_i as unobserved latent variables is induced to define the relation between surogate marker

process and failure times on conditionally independent given with the baseline covariates M_i . The likelihood is formed with

$$[T_i, Y_i | M_i] = \int [T_i, Y_i | n_i, M_i] d[n_i | M_i] = \int [T_i | n_i, M_i] d[n_i | M_i]$$
 (8)

It is required to specify the survival submodel $\begin{bmatrix} T_i, Y_i | M_i \end{bmatrix}$, longitudinal submodel $\begin{bmatrix} Y_i | n_i, M_i \end{bmatrix}$ and latent variable model n_i separately to make relation between the two submodels.

Survival submodel

The survival submodel is defined as

$$\lambda_i(t) = \lambda_0(t) \exp\left\{\alpha^T q(t, n_i) + \gamma^T M_i\right\}$$
 (9)

The term $\lambda_0(t)$ used to define the baseline risk function, and q(.,..) is a vector function of time and the latent variables \mathbf{n}_i , \mathbf{y}^{T} are a vector of regression coefficients associated with

baseline covariates M_i . The term $q(t,n_i)$ is used to define the joint model with $Y_i^*(t)$. It is assumed that the risk of event at time t depends only on the current value of the longitudinal process. There are different option to specify the distribution of

the baseline hazard function $\lambda_0(t)$ under the parametric setup like (the Weibull, the log-normal, the Gompertz, and the Gamma distributions).

Longitudinal submodel

The continuous value of marker's $\left(Y_i^*(t)\right)$ is defined through random effects as :

$$Y_i^*(t) = b_i^T f_i(t); b_i \middle| M_i \sim N(\mu b, \Sigma)$$
 (10)

The term $f_i(t)$ is used to define as the function of time t for q elements. This equation further modified with through consideration of simple linear random effects model for $f_i(t)$ as

$$Y_i^*(t) = b_{0i} + b_{1i}t$$
 (11)

The terms b_{1i} and b_{0i} are defined for slope and subject-specific random intercept respectively. It is feasible to consider random effects term b_i as latent variable n_i [19,17,30,18].

Joint Likelihood formulation and assumptions

The complete log-likelihood conditioned on baseline covariates M_i is defined as

$$l_{c} = \sum_{i=1}^{N} \log \left[h(T_{i}, \delta_{i} | b_{i}, \lambda_{0}, \alpha, M_{i}) \left\{ \prod_{j=1}^{n_{i}} h(Y_{ij} | b_{i}, \sigma^{2} \right\} h(b | \mu_{b}, \Sigma, M_{i}) \right]$$
 Where

$$h(Y_{ij}|b_{i},\sigma^{2}) = (2\pi\sigma^{2})^{-\frac{1}{2}} \exp\left\{-(Y_{ij} - b_{i}^{T} f(t_{ij}))^{2} / 2\sigma^{2}\right\}$$
(13)

is used to define the density of Y_{ij} at time t_{ij} . and

$$h(b_{i}|\mu b, \Sigma, M_{i}) = (2\pi|\Sigma|)^{-\frac{1}{2q}} \exp\left\{-(Y_{ij} - b_{i}^{T} f(t_{ij}))^{2} / 2\sigma^{2}\right\}$$
(14)

is adopted as density of the random effects b_i and the part $h\left(T_i\mathcal{S}_i\left|b_i,\lambda_0,\alpha,\gamma,M_i\right.\right)$ is used as the density for the survival data. It is denoted as

$$\left[\lambda_0(T_i) \left| \exp \left\{ \alpha b_i f_i(T_i) + \gamma^T M_i \right\}^{\delta_i} \exp \left[- \int_0^{T_i} \lambda_0 \exp \left\{ \alpha b_i f_i(u) + \gamma^T M_i \right\} du \right] \right]$$

The random effect part are latent and not observed, the loglikelihood for the observed data is defined as

$$l_0 = \sum_{i=1}^{N} \log \left[\int h\left(T_i, \delta_i \middle| b_i, \lambda_0, \alpha, \gamma, M_i \right) \right] \left\{ \prod_{j=1}^{n_i} h(Y_y \middle| b_i, \sigma^2) \right\} h(b_i \middle| b, \Sigma, M_i) db_i$$
 (15)

It is assumed that the observed marker measurement $Y_i^*(t)$ is dependent on the earlier time measurements

With $\{Y_{i1},.....Y_{ik}\}$ (where $t_{ik} < t$). The latent random effects b_i is considered free from the future time point measurement of $Y_i(t)$.

It is also assumed that the observed marker history $\{Y_{i1},.....Y_{ik}\}$ (where $t_{ik} < t$) and covariates M_i are independent with latent marker process $Y_i^*(t)$ for time point t.

Bayesian methods

The parameters of interest are estimated through Bayesian approach on joint modeling. The prior distribution θ of is defined as $h(\theta|\theta_0)$ through the support of hyperparameters θ . The joint posterior distribution and latent random effects model is defined as

$$h(\theta, b_i | Y_i, M_i, T_i, \delta_i; i = 1, \dots, N)\alpha$$

$$\prod_{i=1}^{N} \left[h(T_i, \delta | b_i, \lambda_0, \alpha, \gamma, M_i) \left\{ \prod_{j=1}^{n_i} h(Y_{ij} | b_i, \sigma^2) \right\} h(b_i | b, \Sigma, M_i) \right] h(\theta | \theta_0)$$
 (16)

The unknown parameters and latent random effects were obtained through Markov chain Monte Carlo algorithm, using the Gibbs sampler [31-34].

The Gibbs sampling procedure provides the iterative sampling from the full conditional distribution of each

parameter given the current assignment of all other parameters and data. The convergence was assessed through the means, medians and variance of the Gibbs samples, and graphs of the empirical distributions. This procedure provide us to borrow strength from experts and incorporate this information in the current analysis and it also permit full and exact posterior inference for any parameter or predictive quantity of interest.

Estimation

The joint distribution with the time-to-event and longitudinal out comes is defined with $P\{u_i, \delta_i, Y_i\}$. It is

assumed that the vector of time independent random effects b_i is shared with longitudinal and survival procedure.

The random effects part is used to make association between the time-to-event and longitudinal outcomes. The correlation between the repeated measurements is considered as conditional independence. It defined as

$$p(U_i, \delta_i, y_i | b_i; \theta) = p(U_i, \delta_i | b_i; \theta) p(y_i | b_i, \theta)$$
 (17)

$$p(y_i|b_i,\theta) = \prod_i p\{p\{y_i(t_{ij})|b_i;\theta\}, (18)\}$$

The term θ is the vector parameter, y_i is the $n_i \times 1$ assigned as longitudinal vector for the responses with i^{th} subject, and

 $p(\cdot)$ provides an appropriate probability density function. It is assumed that the longitudinal and survival submodels both share the same random effects (the shared parameter modeling). The conditional independence assumptions of the joint log-likelihood contribution for the i^{th} is defined as

$$\log p(U_i, \delta_i, y_i; \theta) = \log \int p(U_i, \delta_i | b_i; \theta) \left[\prod p\{y_i(t_{ij}) | b_i; \theta\} \right] p(b_i; \theta) db_i$$
 (19)

The likelihood of the survival section is defined as

$$p(U_i, \delta_i | b_i; \theta) = \left\{ h_i(U_i | M_i(U_i); \theta) \right\}^{\delta_i} S_i(U_i | M_i(U_i); \theta)$$
 (20)

The survival function $h_i(\cdot)$ for $p\left\{y_i(t_{ij})|b_i;\theta\right\}$ as the univariate normal density for the longitudinal responses, and $p(b_i;\theta)$ is the multivariate normal density for the random effects. The log-likelihood function with respect to is a difficult. The challenge is integral with the random effects and define the survival function. However, the Monte Carlo has been attempted under the joint modeling approach [20,35,36] and there are further extension through Laplace approximation [17]. In this work, we attempted and considered the random effects to deal with 'missing data'.

Handling with missing data

The missing data mechanism is defined through consideration of conditional distribution of the time-to-dropout condition to the complete vector of longitudinal outcomes (y_i^0, y_i^m) .

The observed part (consisted with all observed measurement) is defined as and the missing part is defined

$$y_i^0 = \{y_i(t_{ij}) : t_{ij} < T_i, j = 1,....n_i\}$$
 as

$$y_i^m = \{y_i(t_{ij}) : t_{ij} \ge T_i, j = 1,, n_i'\}$$
 (21)

It includes the observed measurements taken until the end of the study. The dropout mechanism adopted under the joint model is

$$p(T_i|y_i^0, y_i^m; \theta) = \int p(T, b_i|y_i^0, y_i^m, \theta) db_i$$

$$= \int p(T, b_i | y_i^0, y_i^m, \theta) db_i \quad (22)$$

$$= \int p(T, b_i | y_i^0, y_i^m, \theta) p(b_i | y_i^0, y_i^m, \theta) db_i$$

The NMAR technique is considered to define posterior distribution of the random effects $p(b_i|y_i^0, y_i^m, \theta)$ tohandle the

time dependent dropout Y_i^m . The single random effect (b_i) component is adopted to address the survival and longitudinal sub-models jointly [37-39]. It is important to make relation between α and missing data procedure. The joint probability of the missing data and the longitudinal processes is defined as:

$$p(U_i, \delta_i, y_i, \theta) = p(U_i, \delta_i, \theta_t) p(y_i; \theta_v, \theta_b)$$

$$= p(U_i, \delta_i, \theta_t) \int p(y_i | b_i; \theta_y) p(b_i; \theta_b) db_i$$
 (23)

The defined parameter of the event time is defined with $\theta=(\theta'_1,\theta'_2,\theta'_3)'$. Further, the random effect part is

defined with $l(\theta_y) = \Sigma_i \log p(y_i; \theta_y)$. It is also applicable for MAR and it is assumed that the dropout data is dependent on observed response. If it is assumed that $\alpha = 0$ then it can served as MCAR mechanism.

The observed data under the consideration of log-likelihood of the complete data is defined as $\left\{y_i^0, y_i^m\right\}$ for the longitudinal outcome:

$$1(\theta) = \sum_{i=1}^{n} \log \int p(U_i, \delta_i, y_i^m; \theta) dy_i^m$$

$$\sum_{i=1}^{n} \log \int \int p(U_i, \delta_i, y_i^0, y_i^m | b_i; \theta) p(b_i; \theta) dy_i^m db_i$$

$$\sum_{i=1}^{n} \log \int p(\delta_i, b_i; \theta)$$

$$\sum_{i=1}^{n} \log \int p(U_i, \delta_i, |b_i; \theta) p(b_i; \theta) db_i$$
 (24)

It is to be noted that the missing longitudinal processes

 y_i^m is involved as the density of the longitudinal sub-model. Incase the dropout is intermittently missing, then the likelihood of a joint model can be easily assigned without considering integration with respect to the missing outcomes. The subject's number of repeated measurement increases then the there is limited effect about miss-specification of the random effect on inference [40-42]. Suppose, in the longitudinal model $m_i(t)$ is linked with the risk of event at time point t with parameter α through the association. It is possible to consider different types of parameterization to link the longitudinal outcomes and risk of dropout.

$$h_i(t) = h_0(t) \exp \left[\gamma' \omega_{i1} + f \left\{ m_i(t), b_i, \omega_{i2}; \alpha \right\} \right], \quad (25)$$

The term $f(\cdot)$ is assigned as a function of the true level of the marker $m_i(\cdot)$, with the random effects b_i and as extra covariates ω_{i2} . The general formulation of α can potentially defined as a vector of the parameters.

Random-effect Component

The longitudinal sub-model through the consideration of the linear predictor of the risk model is defined as

$$h_i(t) = h_0(t) \exp(\gamma' \omega_i + \alpha' b)$$
 (26)

Where is considered to make association between random effect and hazard rate function. It is assumed that the patients who have a lower size of tumor at baseline are more likely to increase in their longitudinal trajectories are less likely to experience the drop out. The random-intercepts and random-slopes incorporated longitudinal sub-model is defined as

$$y_i(t) = \beta_0 + \beta_{1t} + b_{i0} + b_{i1}t + \epsilon(t)$$
 (27)

The relative risk sub-model with the time dependent slope is defined as

$$h_i(t) = h_0(t) \exp\left\{\gamma'\omega_i + \alpha_2\left(\beta_1 + \beta_{i1}\right)\right\}$$
 (28)

For Under this system the relative sub-model is defined as

$$h_i(t) = h_0(t) \exp(\gamma' \omega_i + \alpha_1 b_{i0} + \alpha_2 b_{i1})$$
 (29)

This model is flexible because if we consider, then the model provides the risk depends on the random-slopes component through linear mixed model.

Result

Markov chain Monte Carlo (MCMC) method which assumes multivariate normality has been used to impute

the missing values for all the variables in a data set with arbitrary missing data pattern. Haemoglobin, ECOG

grade and histological grade were used to impute the tumour size. Imputation of CEC values was done from

tumour size. The PROC MI statement is the required statement in the MI procedure for imputation. Available

options in the PROC MI statement are considered: METHOD=MCMC, The CHAIN=MULTIPLE option, this

procedure uses multiple chains and completes the default 200 burn-in iterations before the single imputation.

The 200 burn-in iterations are used to make the iterations converge to the stationary distribution before the

imputation. The option INITIAL=EM was used to get the starting means and covariance from available cases to commence the MCMC process. The resulting imputed CEC values which are almost similar in both the groups in all visits are used for joint

modelling, extended Cox-modelling and Cox regression analysis [43-45].

Table 1: Baseline Characteristics.

Parameters	Statistics	OBD dose level 1	OBD dose level 2						
Baseline Haemoglobin									
>12	$\eta(\%)$	277(25.41%)	277(25.41%)						
<12	η(%)	273(24.59%)	282(25.41%)						
	Histologi	cal grade							
0	$\eta(\%)$	134(25.28%)	131(24.72%)						
1	$\eta(\%)$	255(24.76%)	260(25.24%)						
2	$\eta(\%)$	161(25.16%)	159(24.84%)						
	Baseline ECOG								
0	$\eta(\%)$	174(25.22%)	171(24.78%)						
1	$\eta(\%)$	376(24.9%)	379(25.1%)						
	N	110	110						
	Mean	133.22	133.3						
	STD	18.5	20.97						
	Min	88.2	91.6						
	Max	176.7	181.3						
	N	110	110						
	Mean	3.6	3.12						
Tumor Size	STD	0.4	20.2						
	Min	2.9	2.7						
	Max	4.5	3.6						

Table 1 summarizes baseline characteristics of patients receiving Metronomic Chemotherapy (MC). The baseline Haemoglobin level was less than 12 for 67(62:6%) patients in OBD dose level 1, whereas the baseline Haemoglobin level was less than 12 for 54(47:8%) patients in OBD dose level 2. The distribution of Histological grade is similar for both OBD dose levels. The number of patients with grade 0,1 and 2 are 21 (19.6) , 56 (52.3) and 30 (28.0) respectively in OBD dose level 1 where as the number of patients with grade 0,1 and 2 are 33 (29.2), 44 (38.9) and 36 (31.9) respectively in dose level 2. The Baseline ECOG grade is 1 for 72(67:3%) patients in OBD dose level 1 while it is 78(69:0%) in OBD dose level 2. The average (SD) value of Circulating Endothelial Cell (CEC) Biomarker is reported as 124.3 (15.44) in dose level 1 and 122.4 (15.46) in dose level 2. The average (STD) tumour size is reported as 3.6 (1.14) in dose

level 1 and 3.4 (1.29) in dose level 2.

Table 2: describes the parameter estimates obtained through individual models and joint models. We observe that the CEC

value has indeed a strong association with the risk for death for extended cox regression model.

Table 2: Parameters estimates through individual and joint models.

Parameters	Extended cox model		Joint model		Cox regression	
	HR (95%CI)	P-value	HR (95%CI)	P-value	HR (95%CI)	P-value
Dose	0.883 (0.593,1.316)	0.5402	1.080 (0.966,1.208)	0.1767	0.950 (0.639,1.412)	0.8
CEC Value	1.023(1.012,1.034)	0.0028	1.123(1.061,1.189)	0.0001		

In particular, a unit increase in the CEC value corresponds to a $\exp()=1.023$ times increase in the risk for death (95% CI: 1.012, 1.034).

In the results for the event process for joint model, the parameter in (4.1) that measures the association between the true CEC value and the risk for death. The joint model also finds a strong association between the CEC value and the risk for death, with a unit increase in the marker corresponding to a fold increase in the risk for death (95% CI: 1.061,1.189). Comparing the point estimates and the corresponding 95% confidence intervals from the extended Cox model and the joint model, we clearly observe non-negligible differences. Table 3 summarizes the characteristics of patients receiving Metronomic Chemotherapy (MC) in each visit. At visit 5, Haemoglobin level was less than 12 for 32 (50.8) patients in OBD dose level 1, whereas the baseline Haemoglobin level was less than 12 for 33 (51.6) patients in OBD dose level 2. The number of patients with Histological grade 0,1 and 2 are 17 (27.0), 32 (50.8) and 14 (22.2) respectively in OBD dose level 1 where as the number of patients with grade 0,1 and 2 are 18 (28.1), 32 (50.0) and 14 (21.9) respectively in dose level

2.The ECOG grade is 1 for 47 (74.6) patients in OBD dose level 1 while it is 41 (64.1) in OBD dose level 2. The average (SD) value of Circulating Endothelial Cell (CEC) Biomarker is reported as 122.5 (15.77) in dose level 1 and 123.6 (20.01) in dose level 2. The average (STD) tumour size is reported as 2.7 (0.78) in dose level 1 and 2.6 (0.62) in dose level 2. The average (SD) value of Circulating Endothelial Cell (CEC) Biomarker was 124.3 (15.44), 136.8(15.34) , 151.9(16.11), 133.7(14.69) and 122.5(15.77) in visit 1 ,2,3,4 and 5 respectively in OBD dose level 1 while it is 122.4 (15.46),136.7 (16.38), 155.7(17.10), 136.8(18.64) and 123.6(20.01) in OBD dose level 2. The average (STD) tumour size was 3.6(1.14), 3.4(0.66), 151.9(16.11), 2.9(0.45) and 2.7(0.78) in visit 1 ,2,3,4 and 5 respectively in OBD dose level 1 while it is 3.4 (1.29), 3.3 (0.76), 155.7(17.10), 2.9(0.44) and 2.6(0.62) in OBD dose level 2 [46] (Table 3 (Visit 5)).

Table 3: Summary of Parameters by visit -Imputed data through MCMC method.

			Visit 1			Visit 2			
Variables	Category	statistics	Dose 0	Dose 1	P-value	Dose 0	Dose 1	P-value	
Haemoglobin	> 12	$\eta(\%)$	40(37.4)	59(52.2)	0.02**	50(46.7)	57(50.4)	0.58**	
	12	η (%)	67(62.6)	54(47.8)		57(53.3)	56(49.6)		
Histological grade	0	η (%)	21(19.6)	33(29.2)	0.10**	21(19.6)	26(23.0)	0.65**	
	1	η (%)	56(52.3)	44(38.9)		47(43.9)	52(46.0)		
	2	η (%)	30(28.0)	36(31.9)		39(36.4)	35(31.0)		
ECOG	0	η(%)	35(32.7)	35(31.0)	0.78**	28(26.2)	36(31.9)	0.35**	
	1	η(%)	72(67.3)	78(69.0)		79(73.8)	77(68.1)		
		N	107	113		107	113		
		Mean	124.3	122.4	0.36*	136.8	136.7	0.99	
		SD	15.44	15.46		15.34	16.38		
		Median	124.5	121		139.8	137.6		
		Min,Max	86.8,161.9	76.7,179.1					
Tumour size		N	107	113		107	113		
		Mean	3.6	3.4	0.44	3.4	3.3	0.68	

		SD	1.14	1.29		0.44	0.66	
		Median	4.1	4		3.6	3.6	
		Min,Max	1.1,4.9	1.1,5.0	1.7,4.2	1.0,4.4		
				Visit 3			Visit 4	
Variables	Category	statistics	Dose 0	Dose 1	P-value	Dose 0	Dose 1	P-value
	> 12	η(%)	38(35.5)	54(47.8)	0.06**	31(48.4)	28(40.6)	0.36**
	12	$\eta(\%)$	69(64.5)	59(52.2)		33(51.6)	41(59.4)	
Histological grade	0	η(%)	24(22.4)	26(23.0)	0.88**	13(20.3)	15(21.7)	0.96**
	1	η(%)	46(43.0)	45(39.8)		35(54.7)	38(55.1)	
	2	$\eta(\%)$	37(34.6)	42(37.2)		16(25.0)	16(23.2)	
ECOG	0	$\eta(\%)$	37(34.6)	34(30.1)	0.47**	27(42.2)	21(30.4)	0.15**
	1	$\eta(\%)$	70(65.4)	79(69.9)		37(57.8)	48(69.6)	
CEC		N	107	113	64 69			
		Mean	151.9	155.7	0.16	133.7	136.8	0.28*
		SD	16.11	17.1		14.69	18.64	
		Median	153.7	156.6		134.4	135.3	
		Min , Max	107.9,189.0	104.8,201.8		103.0,170.9	95.3,181.9	
Tumour size		N	107	113		64	69	
		Mean	3.2	3.2	0.26	2.9	2.9	0.41
		SD	0.42	0.48		0.45	0.44	
		Median	3.2	3.2	2.7	2.8		
		Min,Max	1.7,4.1	1.2,4.4	2.0,4.6	1.8,4.3		
				Visit 5				
Haemoglobin	> 12	η(%)	31(49.2)	31(48.4) 0.93**				
	12	η(%)	32(50.8)	33(51.6)				
Histological grade	0	η(%)	17(27.0)	18(28.1)	8.1) 0.98**		8**	
	1	η(%)	32(50.8)	32(50.0)				
	2	η(%)	14(22.2)	14(21.9)				
ECOG	0	$\eta(\%)$	16(25.4)	23(35.9)		0.1	9**	
	1	$\eta(\%)$	47(74.6)	41(64.1)				
CEC		N	63	64				
		Mean	122.5	123.6		0.7	'3*	
		SD	15.77	20.01				
		Median	121.6	121.4				
		Min , Max	83.9,161.2	82.7,178.4				

Tumour size	N	63	64	
	Mean	2.7	2.6	0.82
	SD	0.78	0.62	
	Median	2.4	2.3	
	Min , Max	1.7,5.1	1.7,4.0	

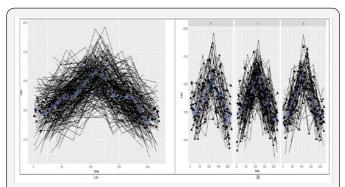


Figure 1: (A) Longitudinal profiles for all patients. The solid lines depict the fitted subject-specific longitudinal profiles. (B)Longitudinal profiles for Histological grade variable. The solid lines depict the fitted subject-specific longitudinal profiles.

interesting characteristic of the Chemotherapy (MC) data is the unusual shapes of the subject specific longitudinal progresses. In particular, Figure 1 A & 1B to Figure 2 C & 2D, exhibit longitudinal profiles for all patients, Histological grade, Baseline Haemoglobin and Baseline ECOG. The solid lines depict the fitted subject-specific longitudinal profiles. Figure 3E, exhibit the Longitudinal response measurements for Biomarker for six randomly selected patients (a=101, b=129, c=211, d=144, e=155 f=179) from the Metronomic Chemotherapy (MC) patient study. The line depicts the fitted subject-specific longitudinal profiles based on the joint model. The patient profile demonstrates highly nonlinear longitudinal profiles for biomarker, which evidently cannot be effectively described by simple structures, such as linear or quadratic progresses in time. This specific problem motivated us to apply joint model that aimed to capture the characteristics of the dataset at hand and reveal related information [47].

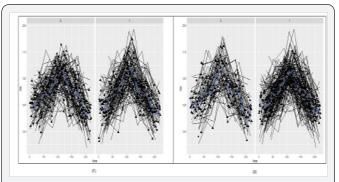


Figure 2: (C) Longitudinal profiles for Baseline Haemoglobin variable. The solid lines depict the fitted subject-specific longitudinal profiles.

(D)Longitudinal profiles for Baseline ECOG variable. The solid lines depict the fitted subject-specific longitudinal profiles

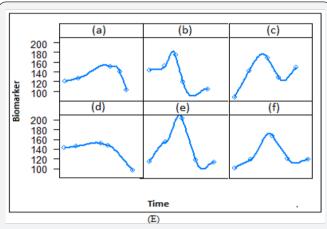


Figure 3. Longitudinal response measurements for CEC Biomarkers for six randomly selected patients.

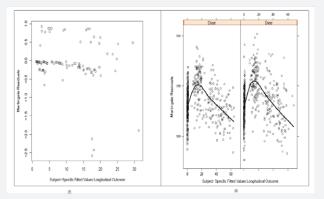
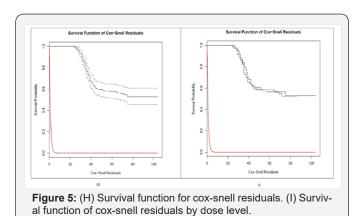


Figure 4: (F)Martigales residuals plot for subject -specific fitted values.

(G)Martingale residuals plot for subject specific fitted values by dose level

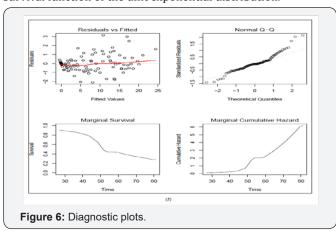
To achieve this goal, we model flexibly the key components of the joint model while making standard parametric assumptions for the remaining parts. To further investigate the suitability of the chosen functional form for the CEC outcome, it is advisable to additionally check for systematic trends in the martingale residuals when we condition on other baseline covariates. Figure 4 (F) demonstrates Martingales residuals plot for subject-specific fitted values for overall treatment effect for Metronomic Chemotherapy (MC) patient study. Figure 4 (G) exhibits Martingale residuals versus the subject-specific fitted values of the CEC per dose level for the Metronomic Chemotherapy (MC) patient study. The black solid lines denote the fitted line. In this figure, Martingale residuals versus the subject-specific fitted values are displayed for dose level 1 on left side and dose level 2 on right side. An another type of residuals for survival

models, associated to the martingale residuals, is the Cox-Snell residuals. For each subject, these are calculated as the value of the estimated cumulative survival function evaluated at the observed event time. This cumulative survival will have a unit exponential distribution. This identity implies that we can check the overall goodness-of-fit by checking whether the Cox-Snell residuals are exponentially distributed. In Figure 5 (H), The black solid line denotes the



Kaplan-Meier estimate of the survival function of the residuals (with the dashed lines corresponding the 95%

pointwise confidence intervals), and the red solid line, the survival function of the unit exponential distribution.



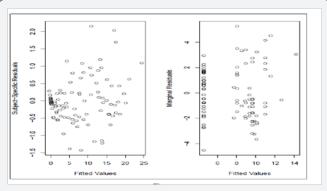


Figure 7: Comparison of Subject specific and Martingal residuals for fitted values.

Figure 5 (I) demonstrates survival function for cox-snell residuals by dose level. The black solid line denotes the Kaplan-Meier estimate of the survival function of the residuals for each dose level, and the red solid line, the survival function of the unit exponential distribution. Figure 6 exhibits diagnostic plots, which is constructed to inspect the _t of joint models with reference distribution of the residuals for the longitudinal process is affected by the dropout. Figure 7 (K) compares the subject specific and Martingale residuals for fitted values.

Discussion and Conclusion

Low-dose chemotherapy drugs are more effective to suppress tumors by restraining tumor vessel growth and

preventing the repair of damaged vascular endothelial cells [48]. High dose chemotherapy drugs like Cisplatin

contributes to serious side effects [48]. The target of MC therapy is the vascular endothelial cells [47]. The growth of new vessels for a long run survival time treated with traditional maximum tolerated dose (MTD) through high dose chemotherapy has been confirmed [43]. The anti-angiogenic plays the important role as clinical potential. The metastasis and the growth of tumor cells depends on neovascularization [45]. The anti-tumor drugs could cause inhibition of tumor neovascularity [46]. The low-dose chemotherapy drugs, as onetenth of the MTD, administered continuously and frequently, could selectively suppress vessel growth in tumor tissues and prevent the repair of damaged vascular endothelial cells (VECs) [48]. This model is appropriate in dose-response modeling having the avoidable level of toxicity in any clinical trial. Based on our knowledge this is the first statistical methodological attempt that has been considered to deal with OBD with timeto-event and longitudinal data in MC trial. It is expected that this above mentioned methods will be useful for OBD detection in MC trials in future as well. The assumption about relation between missing data and unobserved longitudinal process is difficult [42,49]. Our proposed approach proceeds with random effect model. However, the random effect parts assumption and distribution is also difficult and there are previous attempt on that aspect as well. The random effect section is suitable to handle with flexible model through the class of densities [50], and semi-parametric estimation procedure [51]. However, there are some high amounts of standard error generation problem for miss-specification of parameter distribution. The results here suggest that metronomic chemotherapy can be efficacious in improving relapse free survival and survival, and have much less toxicity. This elaborated method can be considered to measure the effect CEC in long run improvement of overall survival (i.e., study initiation to death). This is an initial attempt to work with metronomic chemotherapy on this critical issue that still needs detailed exploration. This is a topic of current exploration. The results presented here to maintain the controlled level of CEC, can be extended to the desire level of PFS and OS through metronomic chemotherapy.

Declaration of interest

The authors declare that there is no conflict of interest that could be perceived as prejudicing the impartiality of the research reported.

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