

Integrating Two Optical Methods to Suppress Diffusive Photons in Ballistic Photons Imaging



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Abstract

A new method to image diffusive media in general and biological tissues in particular, is suggested. The method is an integration of two well-known methods: 1) decreasing the collecting detection angle, and 2) using modulated laser light instead of a stationary beam. The two methods have the same purpose – to suppress the diffusive photons with respect to the ballistic ones. The synergy between the two methods has the potential to improve the imaging considerably. Preliminary analysis show that the system's properties are still challenging – sensitive detectors and high modulation frequencies (>100GHz).

Keywords: Photons; Wavenumber; Ballistic wave; Critical frequency; Stationary; Stationary beam; Scattering; Collimators; Geometrical issue; Detector's solid angle; Dynamic

Introduction

Since biological tissues absorb light in the visible range, light can be a valuable information source for medical imaging [1-4]. The main challenge in using light for tissue imaging is the high scattering coefficient. In the red part of the spectrum, the absorption coefficient (e.g., $\mu_a \cong 0.03\text{cm}^{-1}$) can be negligible compared to the scattering coefficient (e.g., $\mu_s \cong 100\text{cm}^{-1}$). However, beyond the mean free path (MFP) the image becomes blurry. However, the original image can still be recognized until a distance, which is approximately the reciprocal of the reduced scattering coefficient $\mu'_s = (1 - g\mu)\mu_s$, where $g = \langle \cos \theta \rangle$ is the mean cosine scattering angle. In this regime, only diffusive methods can be applied, albeit they suffer from low resolution [5-7].

When the tissue layer is relatively thin, the light can then be separated into ballistic component (i.e., unscattered light), and diffusive component (i.e., scattered light) [8-9]. The diffusive part is scattered in all directions, and therefore the amount detected is proportional to the detector's solid angle

$$I / I_0 = \exp(-\mu_s z) + (\delta\Omega / 4\pi) \exp(-\mu_{eff} z) \quad (1)$$

Where $\mu_{eff} = \sqrt{3\mu_a(\mu'_s + \mu_a)}$, $I_0 \equiv I(z=0)$ and $\delta\Omega / 4\pi \cong (d / 4L)^2$

is the detector's solid angle. Therefore, there is a critical width,

$$Z_c \equiv (\mu_{eff} - \mu_s)^{-1} \ln(\delta\Omega / 4\pi) \quad (2)$$

beyond which the medium can be regarded as a diffusive medium, which is governed by the diffusion equation. When $z < z_c$ the image can be reconstructed using optical method, and relatively high resolution can be achieved. Therefore, there is a clear interest in lengthening z_c . Several methods were suggested to extend this distance[10]:

- decreasing the solid angle of the detector $\delta\Omega$. This is a geometrical issue, which can be addressed by moving the detector away from the source or using collimators [10,11].
- decreasing the scattering coefficient μ_s . This is a spectral issue, which can be addressed by changing the optical wavelength.

There is a third option, which was not addressed: increasing μ_{eff} while decreasing μ_s . This is a challenging task because the region in which $\mu_{eff} \cong \mu_s$ occurs is around 1400nm where the absorption coefficient is extremely high.

In what follows, we suggest a method to increase the attenuation of diffusive photons with minimum effect on the ballistic ones, i.e., to reach the $\mu_{eff} \cong \mu_s$ region without increasing the ballistic photons attenuations.

The idea is to use, what was termed in the literature as “diffusive

photons waves" [5,6]. But unlike Refs.[5,6] here we suggest using this technology to suppress diffusive light. Instead of a continuous light beam, a modulated laser beam is launched into the medium. Therefore, the stationary diffusion equation should be modified to the temporal one

$$-D \frac{\partial^2}{\partial z^2} I + c\mu_a I + \frac{\partial}{\partial t} I = 0 \quad (3)$$

where is the diffusion coefficient. In this case, the light can be separated into a dc (stationary) and an ac (modulated) components

$$I = I_{DC}(z,t) + I_{AC}(z,t) \Re \exp(iKz + i\omega t) \quad (4)$$

where \Re represents the real part. After substituting (4) in the dynamic diffusion equation (3) one finds the dispersion relation

$$DK^2 + c\mu_a = i\omega \quad (5)$$

The result is a complex wavenumber. Consequently, the diffusive wave is more sensitive to modulation than the ballistic wave. Therefore, one can use this property to suppress diffusive photons in comparison to ballistic ones. Going back to the experiment presented in Figure1 but with a modulated laser

source, the AC part of the detected light looks like

$$I_{AC} = I_0 \Re \left[\exp(\mu_s z + ikz - i\omega t + \frac{\delta\Omega}{4\pi} \exp(iKz - i\omega t)) \right] \quad (6)$$

where $K_i = \Im K$ represents the imaginary part of K . Note the difference between the ballistic wavenumber k and the diffusive one K . Since the imaginary part of K is

$$K_i = \sqrt{\frac{c\mu_a}{2D}} \left(\sqrt{1 + \left(\frac{\omega}{c\mu_a}\right)^2} + 1 \right) = \mu_{eff} \sqrt{(\sqrt{1 + \Omega^2} + 1)/2} \quad (7)$$

where $\Omega \equiv \omega / \omega_a = \omega / c\mu_a$. Therefore, the critical distance (2) can be rewritten as

$$z_c(\omega) \equiv (K_i - \mu_s)^{-1} \ln(\delta\Omega / 4\pi) > z_c(0) \quad (8)$$

When $\omega \ll \omega_a \equiv c\mu_a$ then $k_i \cong \mu_{eff}$, however, for $\omega \ll \omega_a = c\mu_a$

$$K_i = \sqrt{\frac{\omega}{2D}} = \mu_{eff} \sqrt{\frac{\omega}{2\omega_a}} \quad (9)$$

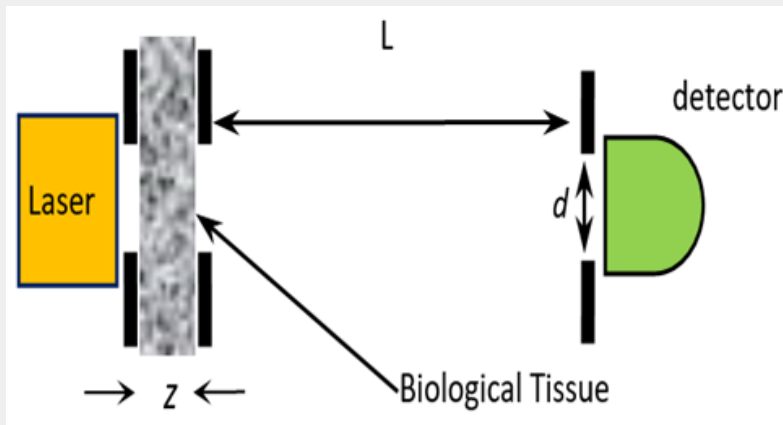


Figure 1: Schematic illustration of the experiment.

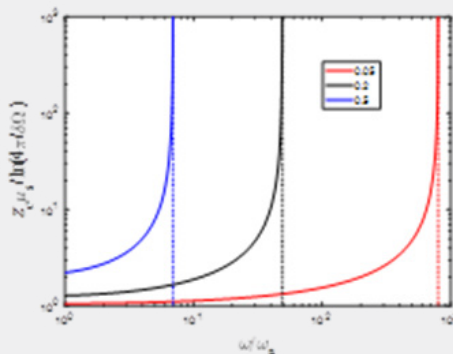


Figure 2: the critical distance as a function of the modulation frequency for different ratios 0.05, 0.2 and 0.5. The vertical dashed lines correspond to the critical frequencies.

The critical distance (normalized to MFP) as a function of the modulation (normalized to $\omega_a \equiv c\mu_a$) frequency is plotted in Figure 2 for different ratios μ_{eff} / μ_s .

For every given ratio μ_{eff} / μ_s there is a critical frequency, around which the critical distance can increase substantially.

$$\omega_c / \omega_a = \Omega_c \cong \sqrt{2\left(\mu_s / \mu_{eff}\right) - 1} - 1 \quad (10)$$

In the important regime, where the ratio is high, the critical frequency is absorption coefficient independent

$$\omega_c \cong 2c\mu_a(\mu_s / \mu_{eff})^2 \cong 2c\frac{\mu_s^2}{3\mu_s} \cong 2c\frac{\mu_s}{3(1-g)} \quad (11)$$

This is a very high critical frequency for wavelengths in the optical domain, around $\omega_c \cong 11 = 100GHz$. This modulation technology is expensive but it is doable.

Moreover, these technologies can be used to improve Signal to Noise Ratio (SNR) when the system is within the ballistic regime. Since the SNR is approximately

$$SNR \cong (4\pi / \delta\Omega) \exp[(K_i - \mu_s)z] \quad (12)$$

then even low frequency modulation improves the SNR by a factor of

$$SNR(\omega) \cong SNR(0) \exp\left[\mu_{eff}(\omega / \omega_a)^2 z / 8\right] \quad (13)$$

Conclusion

To conclude, it is shown that modulated light can be used to suppress diffusive photons with respect to ballistic ones. Consequently, modulated light imaging can be. The SNR can be increased substantially, however, to image thin layers of diffusive

medium, the modulation frequencies should be close to the THz range.

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